

Interest Improved.

S H E W I N G,

From a SMALL TABLE,

By a New, Easy, and Concise Method,

I. RULES for finding the Number of Days from one Month to another, &c. in all the different Cases.

II. The Interest for any Sum, Rate, and Number of Days; likewise its Use in Discompt; also what any Annual Sum is *per Day*, and Daily Sum *per Annum*, &c.

III. A new Method of obtaining the Parts expressing Money; Interest for Years; with the Solution of several new Questions in Stocks, Brokerage, &c.

IV. A Supplement, giving the Construction of the TABLE; where, by one easy Process only, the same is performed by the Pen.

MAKING

The Whole useful for all Academies, Schools, Merchants, Brokers, Clerks, and Accomptants.

By CHARLES BRENT.

L O N D O N:

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T O

William Wilkinson, Esq;

*Agent to his Royal Highness the
DUKE OF CUMBERLAND.*

S I R,

THIS Treatise on the *Interest Table*, of which you was the Inventor, naturally seeks your Patronage.

I shall not use any Encoumisms, setting forth your Sag-

A 2 city

iv DEDICATION.

city and Abilities in Numbers,
etc. it being already known to
many, and from hence will con-
spicuously appear to the World.
I am,

S I R,

Your most humble Servant,

CHARLES BRENT.



P R E F A C E.

AS there are already a Multitude of Treatises on this Subject, some Apology may be expected for the Publication of this.

The most natural is that which is generally understood to all, *viz.* Every Author thinks

A 3 his

his preferable to any before extant.

In respect to the Table, the Dedication sets forth the Inventor, in which I have no farther Concern, than adjoining that Part for the ready obtaining the Number of Days from one Month to another, &c. and giving Rules for Explaining and Illustrating many of its valuable Uses.

The genuine and natural Principles on which it is built, far exceed any thing of the kind

I ever met with; and not only contain all that has been published on this Head, but the Operations resulting therefrom are as easy, more accurate, and, in general, more expeditious, than by Books of ready cast-up Tables; as the Trouble of many Turnings-over and Takings-out of the said Books, are hereby avoided, and which at best admit of a Doubt, whether some Mistake, or Typographical Error may not have escaped Correction.

That
Book will be ready in the month of January.

That I may not be thought prejudiced in Favour hereof, I shall decline saying any Thing further, leaving it to speak for itself, and to the Judgment of all impartial Readers.



T H E



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From

(x)

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Interest

THE
EXPLANATION
A N D
USE of the TABLE.

UNDER the Titles of the Months in the uppermost Row, are the Number of Days from the 1st, or any other Day of *January*, inclusive, to the 1st, or same Day of any subsequent Month exclusive, which is very conspicuous.

Under these again respectively are the Complements to 365, being the Number of Days to *January* following.

To find the Number of Days from any Day of any Month-* inclusive, to the same Day of any subsequent Month exclusive in the same Year.

Subtract the Number in the upper Row under the preceding Month from that in the upper Row under the respective subse-

* If Bills or Notes have been due any Number of Days, the 1st is reckoned inclusive and the Day of Payment exclusive.

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quent Month the Difference is the Answer required.

Thus from the 1st or 10th Day of *January* inclusive (0, being under it) to the 1st or 10th of *June* exclusive are 151 Days, from *February* to *June*, (viz. 31 from 151) are 120, from *April* to *June* 61.

To find the Number of Days in any one Month required.

Subtracting the Number of Days under the said Month in the upper Row from that of the next subsequent, gives the Answer.

Thus 31 the Number of Days under *February* subtracted from 59 under *March*, gives 28 the Answer required.

In Leap-Years you must add a Day more, if your Inquiry begins in *January*, or *February*, and the subsequent Month be *March* or after, otherwise not.

If the Number of Days required be from different Days of the Months, suppose from the 3d of *January* inclusive, to the 17th of *June* exclusive.

From the 3d of *January* to the 3d of *June* are 151 Days as before. But as there are 14 Days more from the 3d to the 17th, by adding 14 to 151, gives 165, the Answer required.

If it be from the 17th of *January* to the 3d of *June*, from the 17th of *January* to the 17th of *June* are 151, but that being 14 Days too much, subtract 14 from 151 gives 137 for Answer, &c. If

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If the Number of Days required be from any Month to that of any other in the ensuing Year, suppose from *November* to *March* following.

To 61 in the second Row, under *November*, (the Days wanting to the 1st of *January*) add 59 in the upper Row under *March*, (the Days from the 1st of *January*) gives 120, the Answer required.

If the Days of the Month be different, you must proceed as before, p. 2.

It must be observed that when the following Year is Leap-Year, and the Month in the said following Year is after *February*, to add a Day more otherwise not.

If there are any Number of Days, *viz.* 117 to be added to those of any Month, suppose *May* the 11th to find what subsequent Month and Day it will fall on.

To 120 under *May* in the upper Row, add 117, which makes 237, the next less is 212 under *August*, this taken from 237, leaves 25, *viz.* twenty-five Days beyond the 11th of *August*, which is *September* the 5th following, or as 237 wants but 6 Days of 243 to fall on the 11th of *September*, subtracting 6 from the 11th, gives the 5th as before.

If the Number of Days given to be added had exceeded 245 in the under Row, suppose 342 subtracting 245 therefrom, and to the Remainder 97 adding 11, the Number of Days

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in *May*, this Sum 108 sought in the upper Row gives the 18th of *April* in the following Year, the like with others.

If there are any Number of Days to be subtracted from those of any Month, suppose 117 from the 11th of *May* as above, to 120 in the upper Row under *May*, add 11 the Days advanced therein next from the Sum, 131, subtract 117, gives * 14 *January* preceding.

If the Number of Days given had exceeded 131, suppose 342 subtract 131 therefrom, and the Remainder 211 from the next greater in the under Row which is here 214 under *June*, the last Remainder 3 gives *June* 3 of the preceding Year, the like with others.

In the Columns of the Interest Table Part the 1st, under Prin. (which signifies Principal) where the Place of the Interest is but one, as against Pence, there five Cyphers are supposed before it, where there are two Places, (as mostly against Shillings) four Cyphers, three Places, three Cyphers, four Places two Cyphers are respectively supposed prefixed (or before them,) but in the second Part of the Table they are to be taken as there express'd, and every of which in both Parts of the Table expresses the Interest of its respective Principal for one Day at 5*l.* per

* Exclusive if the 11th of *May* be inclusive, or inclusive if the 11th of *May* be exclusive.

Cent.

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Cent. per Annum. This will be found very familiar and easy by the following Examples.

EXAMPLE I.

WHAT is the Interest of 7*l.* for 365 Days at 5*l.* per Cent. per Annum.

In the Table against 7*l.* is 959
Multiply by 365
 4795
 5754
 2877
Product | 350035

As the Interest taken out of this 1st Part of the Table with Cyphers pre-supposed, must always consist of six Places (See p. 4.) so the Product must likewise consist of six Places for Parts, and where defective a Cypher or Cyphers must be prefix'd or suppos'd, to make 'em up so many. — The Product in this Example is just the Number.

Next to Value this (or any other) Product, the Digit in the sixth Place to the left Hand must always be doubled, which will then be Shillings, and the two next Places to the right Hand of it are Farthings, bating one out of every 25. So in this Example, 3 doubled

B 3 gives

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gives 6 Shillings, and the two next Places, *viz.* 50 bating one out of each 25, gives 48 Farthings, or one Shilling, making for the Interest required 7 Shillings, the other Figures being of no Value.

Hence 'tis plain, that 5 possessing the 5th Place to the left Hand (being the first Place of Farthings) is in Value one Shilling, and when no more Places succeed, a Cypher must always be suppos'd, or put after it to the Right Hand (as indeed to any other Digit in the same Place), three Places being requisite for valuing of Money.

E X A M P L E II.

WHAT is the Interest of 54*l.* for 98 Days, at 5*l.* per Cent. per Ann.

Against 54*l.* is (for Interest of one Day) 7397
Multiply by 98

$$\begin{array}{r} 59176 \\ 66573 \\ \hline \text{Product } |724906 \end{array}$$

Here 7 doubled gives 14 Shillings, and the following 24 for Farthings; but when the Digit succeeding those for Farthings is 5 or upward, they without sensible Error, may be made one more, which here being 9, they become 25, and one bated gives 24 Farthings or

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or 6*d.* making the Interest required 14 Shillings and 6*d.*

EXAMPLE III.

WHAT is the Interest of 5*l.* for 47 Days, at 5*l. per Cent. per Annum.*

Against 5 <i>l.</i> is	—	—	685
		47	47
		4795	4795
		2740	2740
			1032195

Here are but 5 Figures in the Product, which, as there must always be six, (See Ex. p. 5.) a Cypher must be put or suppos'd before the 3 to the left Hand, which shews there is nothing to be doubled for Shillings, and the following 32 are Farthings, bating one as before for 25, gives for Answer 31 Farthings, or 7*d.* $\frac{3}{4}$, the Digit following the Farthings when under 5, (as here) may be omitted.

EXAMPLE IV.

WHAT is the Interest of 8*l.* for a Day at 5*l. per Cent. per Annum.*

Against 8 <i>l.</i> is	—	—	1096
------------------------	---	---	------

Which multiplied by 1 is still the same, but as there must always be six Places in the Product, so here must be two Cyphers put or

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or suppos'd before it, (See p. 4.) so that I now in the 3d * Place, will be but one Farthing *per Day*, and the following Digits make it a little more. But if it be required for 365 Days, then — — —

$$\begin{array}{r} 1096 \\ \text{Multiply'd by } \underline{365} \\ 5480 \\ 6576 \\ 3288 \\ \hline 400040 \end{array}$$

Here are six Places in the Product, so that the first Digit 4 being doubled gives 8 Shillings, the other Figures being of no Value.

EXAMPLE V.

WHAT is the Interest of 26*l.* for 287 Days at 5*l. per Cent. per Annum.*

Against 26*l.* is — — —

$$\begin{array}{r} 3562 \\ 287 \\ \hline 24934 \\ 28496 \\ 7124 \\ \hline 1022294 \end{array}$$

Here in the Product are seven Places, therefore six are cut off, as it must always be when

* Note, where the Places in the Table, or any Product are but 3, or under, there the Interest is under a Farthing, as 3 Cyphers must be, suppos'd or prefix'd to them &c.

the

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the Places are more, and those to the left Hand will then be Pounds Sterling, so that the Interest will here be $1\ l.\ 0\ s.\ 5\ d.\ \frac{1}{4}$ bating one from 22, as it is so near 25. Note, As 0 is in the first Place, there is nothing to be doubled for Shillings. (See Ex. III. p. 7.)

E X A M P L E VI.

W H A T is the Interest of $63\ l.$ for 229 Days at $5\ l.$ per Cent. per Annum.

Against $63\ l.$ is	—	—	8630
		229	<hr/>
		7767	
		1726	
		1726	
		1	<hr/>
		976270	

Here again is 1 l. next 9. doubled gives 18 Shillings; and 73 Farthings, bating 3 from 76 for the 25's. But seeing that 5 in the 5th Place to the left Hand (See Ex. I. p. 6.) makes a Shilling more, therefore subtracting 5 from the 7, and prefixing 2, the Remainder, to the 6, it will then be 26 for Farthings, and bating 1 for 25, the remaining 25 will be $6\ d.\ \frac{1}{4}$, and the Interest $1\ l.\ 19\ s.\ 6\ d.\ \frac{1}{4}$.

E X A M-

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E X A M P L E VII.

WHAT is the Interest of 7*l.* 13*s.* 4*d.*
for 365 Days at 5*l* per Cent. per Ann.
Against 7*l.* (as in Ex. I.) is 959, and as there
are 3 Cyphers suppos'd prefix'd (See p. 4.
which here for Illustration let be supplied
Thus |000959
Next against the 13*s.* is 89, which
with 4 Cyphers (p. 4.) is |000089
And against 4*d.* is 2 with 5 Cyphers |000002
Sum |001050

From whence it is plain that 89 and 2, *viz.*
91 being added to 959 (which may be done
mentally) is 1050

There being (*per* p. 4.) Two Cyphers sup-
posed,

Therefore 1050*
 Multiply'd by 265
 525
 630
 315
Which (*per Rule* p. 5.) is 7*s.* 8*d.* |383 50

In the first Column under Principal, 6*d.* 7*d.*

* When a Cypher, or Cyphers are at the Right Hand
of the Interest or Product they may be omitted, and so
many places less, accounted for in the said Product.

8*d.* and

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8d. and 9d. are (for the * Conveniency of having Pounds only in the 3d Column) left out; but the Expressions of Interest answering to them, are easily found. Thus

	d.	d.	d.
	4 & 2	are 2 & 1 viz. 3	is for 6
Against	$\left\{ \begin{matrix} 5 & 2 \\ 5 & 3 \\ 5 & 4 \end{matrix} \right.$	$\left\{ \begin{matrix} 3 & 1 \\ 3 & 2 \\ \text{ditto} \end{matrix} \right.$	$\left\{ \begin{matrix} 4 \text{ ditto} \\ 5 \text{ ditto} \\ \text{ditto} \end{matrix} \right.$
			7 8 9

N.B. Against $3d\frac{1}{2}$ in the Table is 2, which is extremely near being exact, which also may be taken for 3 d. or 4 d.

‡ 3.	Therefore is more exactly for 5 d.	$\frac{1}{4}$
† 5.	Ditto.	8 d. $\frac{3}{4}$
6.	Ditto.	10 d. $\frac{1}{2}$

Though these last are the most accurate Expressions and may be found to accord in Questions where Half-pence and Farthings are given, they, however may be omitted, and the nearest Expression taken, formed as at first above from the Table, from whence in the Answers no Error will arise in the Value of the Money.

* Otherwise the Shillings wou'd mix with the Pounds.

† Taken also for 6 d. as above.

† Ditto 8 d. or 9 d. Ditto.

|| Ditto 10 d. or 11 d. Ditto.

EXAMPLE

EXAMPLE VIII.

W H A T is the Interest of 53*l.* 7*s.* 9*d.*
for 134 Days at 5 per Cent. per Ann.
Against 53*l.* is — — 7260
Against 7*s.* is 48 and 5 for 9*d.* 53*
Sum 7313
134
29252
21939
7313
979942

Viz. 19*s.* 7*d.* $\frac{1}{4}$ (See Example 2, p. 6.) — }

These Examples being fully sufficient for explaining the Use of the first Part of the Table, I shall next proceed to that of the Second, which will be always when the Principal given is 73*l.* or upwards.

EXAMPLE I.

W H A T is the Interest of 73*l.* for 125 Days at 5 per Cent. per Ann. against 73 is 101 and as 125 is the greater Number, place that first thus

Multiply'd by	—	125
	—	101
	—	125

* Which might have been added mentally.

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Here as there are but two Places of Parts in this Part of the Table which are to be taken as express (see *Def. p. 4.*) there must be but two Places cut off in the Product, whence those to the Left-hand (as before in the first Part) will be Pounds *Sterling*, the 2 in the first Place to the Left-hand of the Parts doubled, gives four Shillings, and the 5 succeeding a Shilling more, (see *Ex. 1. p. 8.*) making the Interest required 1*l. 5s. 0d.*

From hence it is conspicuous that every Interest in the second Part of Table, as well as in any Product therefrom (excepting against 7300*l.* and where it ends with 0) must have a Cypher supposed or put after it to the Right-hand for Valuing, the same in Money. See *p. 5.*)

EXAMPLE II,

W	HAT is the Interest of 211 <i>l.</i> for 182 Days at 5 <i>l. per Cent. per Ann.</i>
Against 211 <i>l.</i> is 29 Therefore	182 <i>l.</i> Multiply'd by 29 <hr/> 1638 364

viz. 52*l. 15s. 7d. $\frac{1}{4}$* which is } 52|78+
very conspicuous
† A Cypher supposed.

C

EXAMPLE

EXAMPLE VIII.

W H A T is the Interest of $53 l. 7 s. 9 d.$ for 134 Days at 5 per Cent. per Ann.

Against $53 l.$ is	—	—	7260
Against $7 s.$ is 48 and 5 for 9 d.			<u>53*</u>
	Sum	7313	
		134	
		29252	
		21939	
		7313	
Viz. 19 s. 7 d. $\frac{1}{4}$ (See Example 2. p. 6.)	—	3	<u>979942</u>

These Examples being fully sufficient for explaining the Use of the first Part of the Table, I shall next proceed to that of the Second, which will be always when the Principal given is $73 l.$ or upwards.

EXAMPLE I.

W H A T is the Interest of $73 l.$ for 125 Days at 5 per Cent. per Ann. against 73 is 101 and as 125 is the greater Number, place that first thus

Multiply'd by	—	125
		101
		125

* Which might have been added mentally.

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Here as there are but two Places of Parts in this Part of the Table which are to be taken as express (see Def. p. 4.) there must be but two Places cut off in the Product, whence those to the Left-hand (as before in the first Part) will be Pounds *Sterling*, the 2 in the first Place to the Left-hand of the Parts doubled, gives four Shillings, and the 5 succeeding a Shilling more, (see Ex. 1. p. 8.) making the Interest required 1*l.* 5*s.* 0*d.*

From hence it is conspicuous that every Interest in the second Part of Table, as well as in any Product therefrom (excepting against 7300*l.* and where it ends with 0) must have a Cypher supposed or put after it to the Right-hand for Valuing, the same in Money. See p. 5.)

EXAMPLE II,

WHAT is the Interest of 2117*l.* for 182 Days at 5*l.* per Cent. per Ann.

Against 2117 <i>l.</i> is	29	Therefore	182 <i>l.</i>
	Multiply'd by		29
			—
			1638
			364

viz. 52*l.* 15*s.* 7*d.* $\frac{1}{4}$ which is
very conspicuous

† A Cypher supposed.

C EXAMPLE

EXAMPLE III.

WHAT is the Interest of 2920*l.* for
182 Days at 5*l. per Cent. Ann.*

Against 2920 <i>l.</i> is 40 therefore	182
—	Multiplied by
	<u>40</u>

Viz. — — 72*l.* 16*s.* 0*d.* 72|80

Against 7300*l.* is 1*l.* which is the Interest of the said Sum for one Day, and if required for any number of Days will be so many Pounds Sterling. And though this Table extends no farther than 7300*l.* yet it is made general, and for any Sum as will appear in the following Examples, which treats of both Parts of the Table together, &c.

EXAMPLE I.

WHAT is the Interest of 200*l.* for 73 Days at 5*per Cent. per Ann.* when the Principal given (as before, p. 11.) exceeds 72*l.* you must always seek it in the second Part of the Table, and if not found exact, take the next less and the Interest against it, then subtract the said next less from the given Principal, and seek the Remainder if under 73*l.* in the first Part of the Table, taking out also the Interest against the same. These Interests added together, will be that of the given Principal for one Day, and which

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which multiplied by the number of Days gives the Answer required. In this Example the next less nearest number to 200*l.* in the second Part of the Table is 146, and the Remainder 54. Then against 146 in the second Part is — — 02
and 54 in the 1st. (*see p. 4*) 007397
Their Sum (which now consisting of
six Places, there must be so many
in the Product for Parts) 027397
multiplied by ———— 73
 82191
 191779
 1999981

Here the Interest is first 1*l.* and valuing the others they make 19*s.* and 49 for Farthings at first Sight, but seeing that 9 follows the Place of Farthings (as also 8 that again) they must *per Ex. 2. p. 6.* be made one more when they will become 50. *viz.* 1*s.* so that the true Interest becomes 2*l.* as required.

It may be observed that the 0 before the 2 taken out of the second Part might have been supposed, as also that when the Number taken out of the first Part consists of four Places they may be immediately placed after those taken out of the second Part, &c.

EXAMPLE II.

VVHAT is the Interest of 152*l.* for a Day at 5 per Cent. per Ann.

Against 146*l.* Part 2d. is (as before) 02
and against 6 the Remr. Part 1st. 000822

020822

Here it may be observed, that when the Interest taken out of the first Part of the Table, consists of three Places, they are to be placed after the Interest taken out of the second Part, with one Cypher intervening.

EXAMPLE III.

VVHAT is the Interest of 146*l.* 13*s.* 0*d.*
for a Day at 5 per Cent. per Ann. against 146*l.* is — — 02
and against 13*s.* (See Def. p. 3.) 000089

020089

Here it may be also observed, that when the Interest taken out of the 1st. Part of the Table consists of two Places, they are to be plac'd after that taken out of the 2d. Part with two Cyphers intervening.

N. B. All the Interests taken for a Day may be valued by *p.* 5. &c.

E X A M P L E IV.

WHAT is the Interest of 146*l.* 1*s.*
for a Day at 5 per Cent. per Ann.
against 146*l.* — — |02
And against 1*s.* (See Def. p. 4.) 000007
|020007

Here it is lastly to be observ'd, that when Interest taken out of the 2d. Part of the Table, consists but of one Place, it is to be plac'd after that taken out of the 2d. Part with three Cyphers intervening.

Hence follows this general Rule, that when the Places of Interest taken out of the first Part are less than four, by prefixing Cyphers to make them that Number, they may be immediately plac'd after those taken out of the second Part.

E X A M P L E V.

WHAT is the Interest of 847*l.* 12*s.*
6*d.* for a Day at 5 per Cent. per Ann.
Against 803*l.* is 11. against 44. is 6027. and 3 for 6*d.* Interest ditto } 116030*

* Which o may be omitted, See p. 10.

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E X A M P L E VI.

W H A T is the Interest of 809 l. 0 s.
7 d. for a Day, at 5 per Cent. per Ann.
Against 803 l. is 11. against the
Remainder 6 is of 822. and 4. for } 110826.
7 d. the Interest, *ditto* }

E X A M P L E VII.

W H A T is the Interest of 803 l. 17 s.
8 d. for a Day at 5 d. per Cent. per
Ann. against 803 l. is 11 against
17 s. is 116 and 5 for 8 d. Inter- } 110121
est, *ditto*. —

E X A M P L E VIII.

W H A T is the Interest of 1022 l. 5 s.
9 d. for a Day at 5 per Cent. per Ann.
Against 1022 l. is 14, against 5 s. }
is 34 and 5 for 9 d. Interest, *ditto*. } 140039

E X A M P L E IX.

W H A T is the Interest of 219 l. 1 s.
10 d. for a Day at 5 per Cent. per Ann.
Against 219 l. is 03. against 1 s. }
is 7 and 6. for 10 d. Interest, *ditto*. } 030013

Which

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Which Interests as indeed all others are taken out with little more Trouble than a bare Inspection. (*See Rule p. 17.*)

The following Examples exhibit the Method of making the Table general for all Sums as mention'd (*p. 12.*)—

EXAMPLE I.

WHAT is the Interest of 8760*l.* for a Day at 5*l. per Cent. per Ann.* Seek in the second Part of the Table the next less * Principal to the first three or four Places of the Principal given, which set directly under it, beginning at the first Place to the Left-hand.

Thus the given Principal is 8760
Next less Tabular, *ditto* 8, 6 against it | 12

Here it is to be observed, that the given Principal is ten Times as much as the Tabular Principal, it extending one Place farther to the Right-hand. The Interest therefore will be ten Times as much as at first taken out of the Table, which is made by separa-

* Which at most consists but of four Places.

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ting one † Place thereof to the Left-hand
Thus $1\frac{1}{2}$, whence the Place so cut off be-
comes an Integral or 1l. Sterling , and the
Interest required $1\text{l. } 4\text{s.}$.

E X A M P L E II.

IF the given Principal be 87600*l.*
The Tabular *ditto* as before is 876

Here as the given Principal extends two
Places to the Right-hand, it is an hundred
Times the Tabular Principal; therefore two
* Places of the Interest must be separated or
cut off to the Left-hand when the said $1\frac{1}{2}$
will become Integral, and the Interest 12l.
per Day as required.

E X A M P L E III.

IF the Principal be 876000*l.*
Tabular, Number 876

Here as the Principal is three Places ex-
tended beyond the Tabular Number, there
is required three || Places to be separated to
the Left-hand for the Interest, which is done

† Which is multiplying the Expression of Interest by
10 and reversely if a Tenth of $1\frac{1}{2}$ the Interest of
876*l.* be required, it will be $1\frac{1}{2}$. which is dividing
the said Expression by 10. and will be the Interest of
876*l.* *viz.* one Tenth of 8760*l.* &c.

* Which is multiplying 100
|| Ditto 1000

by

by annexing 0, to the Right-hand of 12. making 120 which is the Pounds *Sterling*, per Day, the Interest required, and in general so many Places as the Integral given Principal extends beyond the Tabular Principal, so many Places must be cut off to the Left of the Tabular Interest for Integers, by annexing Cyphers to the Right-hand, when requisite.

EXAMPLE IV.

WHAT is the Int of 987763 l. for a Day,
at 5 per Cent. per Ann.

Tabular Number	949	against it 13
which per last, is 130		
The Remainder is	38763 *	
Tabular Number	3869	against it,
53 which per Ex. 1. makes		5 3
The Remainder is	73	against
which is now only the Parts, viz.		01
All added together make	135 31	
+ viz. 135 l. 6 s. 2 d. $\frac{1}{2}$.		

* Bringing down the remaining Figures or Places of the given Principal.

† See p. 13.

22 *INTEREST* Improved.

E X A M P L E V.

WHAT is the Interest for 22 Days at 5 per Cent. per Ann. of 100000 l.

Tabular Number	949 gives 13
Remainder, &c.	5100 †
Tabular Number	5037 gives 69
Remaind. in Part 1st	63 gives 008630
The several Int. added tog. make 13 69863*	
Multiply by	22
	2739726
	2739726
viz. 301 l. 75. 4 d. $\frac{3}{4}$	— 301 36986

If there had been Shillings, &c. given with the 5 last Examples, the several Interests might have been found with Ease by the Rules a foregoing. But these great Principals are given for the Illustration of making the Table general, as they seldom (or never) happen in Business.

Hitherto the Interests have been all found at 5 per Cent. the following Examples will clear up the Method of finding it for all Rates.

† See Page 21.

|| Here 8630 might have been plac'd after 69. (See Page 15.)

* The o is omitted. (See Page.)

R U L E.

MULTIPLY the Interest found first at 5*l.* per Cent. for a Day by double, the Rate required, next separate from the Product one Place more for Parts than were before, supposing Cyphers prefix'd when requisite, (*See Example I. p. 5.*) which will then consist of seven Places (excepting where the second Part of the * Table is alone concern'd.)

E X A M P L E I.]

WHAT is the Interest of 44*l.* at $1\frac{1}{2}$ per Cent. per Ann. for a Day, against 44*l.* is 6027*l.* which multiply'd by 3, double the Rate, gives 10018081 here for illustration the two Cyphers, are prefix'd to make 7 Places, but it may be observ'd that when the last Place to the Right-hand is under 5, it may be omitted; when it is 5 or above, the Place before it or 6th to the Right-hand may be made one more, and only operate for six Places as in all the preceding Examples where the first Part of the Table has any Concern, (*see p. 13, 14.*)

* See p. 12, 13.

EXAMPLE II.

WHAT is the Interest of 6*l.* for a Day at $2 \frac{1}{2}$ per Cent. per Ann. against 6 is 822 which multiply'd by 5. the double Rate gives 4110 here three Cyphers must be suppos'd to make the Places 7. but 0 in the last Place to the Right-hand may be * omitted, working only for six Places in the Product, it may also be observed, that $2 \frac{1}{2}$ per Cent. is half 5 and that 411*l.* is likewise half the Interest taken out of the Table.

EXAMPLE III.

WHAT is the Interest of 60*l.* for a Day at 2*l.* per Cent. per Annum. against 60*l.* is 8219 multiply'd by 4 gives 32876 for Answer, here omitting 6 the last Place to the Right-hand, and adding 1 to the 7 before it, you may operate with 3288 for six Places and pursuing this Method, you will have no Errors of Value in all the Operations, &c.

* See Note, p. 10.

EXAM-

EXAMPLE IV.

WHAT is the Interest of 6*l.* for a Day at $2 \frac{1}{4}$ per Cent. per Ann. Interest against 6*l.* is 822 double Rate 4 $\frac{1}{4}$.

Multiply by $\frac{4}{3288}$

$\frac{1}{2}$ Interest against 6	<u>411</u>
Interest required	<u>3699</u> *
Or	<u>370</u>
Or	<u>37</u> †

EXAMPLE V.

WHAT is the Interest of the last Example for a Day at $2 \frac{1}{4}$ per Cent. &c. Interest as before 822 double Rate 4 $\frac{1}{4}$.

$\frac{4}{3288}$
 $\frac{1}{2}$ Int. against 6 205 *

Answer. 3493 which will be 349 for 6 Places *per* foregoing.

* With three Cyphers suppos'd prefixt.

|| For 6 Places.

† For 5 ditto. See Note, p. 10.

• The 5 might have been made one more, as it may always when the Remainder is Half, or above Half the Divisor, which is done in this last Example.

EXAMPLE VI.

WHAT is the Interest of the last Example for a Day at $3 \frac{7}{8}$ per Cent. per Annum.

Interest as before 822 and double Rate $7 \frac{3}{4}$.

	7
	<hr/>
	5754
$\frac{1}{2}$ Int. against 6	411
$\frac{1}{2}$ this again	206
	<hr/>

viz. 637. the Answer

for 6 Places, &c.

In the preceding Examples, the fractional Parts of the Interests (for the double Rates) have been taken $\frac{1}{3}$, $\frac{1}{4}$, $\frac{3}{8}$. (scarce any other being in use) But in different Cases, or where the Tabular Interest is an odd Number, it will be as well to double the Tabular Interest at 5 per Cent. &c. (or take the Interest of double Principal) when multiplying by the Rate given still having Regard to 7 Places in the Product, &c. (See p. 23.) and operating as in other Respects *per* the foregoing, gives the Answer required.

EXAMPLE VII.

WHAT is the Interest of 7*l.* for a Day at 1*l.* and $\frac{1}{16}$ per Cent. per Annum.

Against

Against 7*l.* is 959 double thereof 1918

$\frac{1}{16}$ — 119 and 14 remaining, here the 9 may be made one more (See p. 25) when it will be 120, which added to 1918 makes 2038, and by p. 24. it will be 204 for 6 Places in the Product, the like with others.—But in the 2d Part of the Table as the Places of Interest are but two a Cypher must be put, or suppos'd prefijxt to make them 1 more for 3 in the Product, (See p. 21) except against 7300*l.* where the Interest is Integral, which will then become the first Place of Parts, and only one Place required in the Product, but both these is when the double of the Rate to be reduc'd unto is only Pounds Sterling, otherwise it will be varied as in the foregoing; which the ensuing Example will make easy.

E X A M P L E I.

W H A T is the Interest of 876*l.* for a Day at 1*l.* per Cent. per Annum.

Against 876*l.* is 12 multiply'd by double Rate, viz. 2 2

(See p. 21.) viz. 5*d* $\frac{1}{4}$ $\overline{024}$ Answer required, and 3 Places of Parts for the Product.

E X A M P L E II.

W H A T is the Interest of 1825*l.* for a Day at 1*l.* per Cent. per Annum.

D 2 Against

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Against 1825*l.* is 25 double the Rate 2.
Multiply'd by 2

Viz. 1 Shill. — — 1050

which last, omit then 05 Answer required,
and 2 Places for the Product. (See Note p. 10.)

E X A M P L E III.

W H A T is the Interest of 7300*l.* for a
Day at 1 per Cent. per Annum.

Against 7300*l.* is 1 an Integral or 1*l.*
Multiply by 2 double Rate.

Viz. 4 Shillings — — 12 Answer. With one
Place of Parts for the Product. (See p. 24.)

Here it may be observ'd, if the Interest of
a Tenth of 7300*l.* be requir'd, viz. 73*l.*
against it in the Table is 110 Parts, and if the
Interest be at 5*l.* per Cent. the Value (by p.
5.) will be 2 Shillings, the Tenth of 1*l.* a-
gainst 7300*l.* — If the Interest of an hun-
dredth Part of 7300*l.* or Tenth of 73*l.*
viz. 7*l.* be required against it in the Table
is 101 Parts, which is the tenth Part of 2
Shillings, or hundredth Part of 1*l.* — From
whence it is very plain, that the Expression
for a tenth Part of 1*l.* (the Interest of 7300,
&c.) becomes 1 in the first Place of Parts to
the left Hand, (See Note * p. 18, 24.) and
for an hundredth Part thereof it becomes 101
the 1 being then in the second Place of Parts
with a Cypher prefixt for that Purpose, &c.

E X A M-

E X A M P L E IV.

WHAT is the Interest of 949*l.* for 47 Days at 3*l.* $\frac{1}{2}$ per Cent. per Annum.

Against 949*l.* is 13 doubled 026 with o prefixt.

Double Rate 7 Mult. by 3

Int. of a Day 1091 &c. 078
12*

$$\begin{array}{r} 1091 \text{ Int. for a Day.} \\ 47 \\ \hline 637 \\ 364 \\ \hline 41277 \end{array}$$

Here as there was at first but three Places of Parts for the Interest of a Day, so there must now be no more in the Product, when the Interest required will be 4*l.* 5*s.* 6*d.* $\frac{1}{2}$.

* Half of 026 the double Interest.

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E X A M P L E V.

WHAT is the Interest of the last at 4*l.*
 $\frac{1}{4}$ per Cent. &c.

Double, &c. is as before.

026

$$\begin{array}{r}
 4 \\
 \hline
 104 \\
 65 \\
 \hline
 1105 \\
 47 \\
 \hline
 7735 \\
 4420 \\
 \hline
 51935
 \end{array}$$

Viz. 5*l.* 3 $10\frac{1}{3}$ nearly

Here after dividing 026 by 4, there remain'd 2, to which annexing a Cypher and dividing on it gave 5 for another Place of Parts, which then became 4, and requir'd so many to be cut off for Parts in the Product, And this (if the Quotient does not terminate before) will be found necessary to be carried on to 6 Places but never more, (by adding a Cypher to each Remainder) when if the Remainder be Half or above Half the Divisor, the last Place must be made an Unit more, otherwise not.

MAZ

E X A M-

E X A M P L E VI.

W H A T is the Interest of the last at $5l.$
 $\frac{1}{12}$ per Cent. per Annum.

Double as before is	1026	$16) 026 (1625$
	$\frac{5}{\overline{130}}$	100
$\frac{1}{12}$ of 026	1625	40
	$\frac{\overline{131625}}{47}$	80
	$\frac{47}{921375}$	47
	$\frac{526500}{}$	

Viz. $6l. 3 \frac{3}{4}$ nearly $\frac{6}{1} 186375$ Answer.

E X A M P L E VII.

W H A T is the Interest of $73l.$ for a Day
 at $1l.$ per Cent. per Annum..

Against $73l.$ at $5l.$ per Ct. is 01 doubled &c.	002 the Ans.
Against $1 \frac{1}{2}$ per Ct. per the foregoing it will be	003
Against $1 \frac{1}{4}$ ditto	0025
Against $1 \frac{1}{8}$ ditto	00225
Against $1 \frac{1}{16}$ ditto	002125
Making 3, 4, 5, and 6, Places for the Product respectively, &c.	

EXAMPLE VIII.

WHAT is the Interest of 7300*l.* for a Day at 6*l.* $\frac{1}{4}$ per Cent. per Annum.

Against it is 1 which doub. is 12 and is first Pl.

6 (of Parts.)

$$\begin{array}{r} \frac{1}{4} \text{ of } 2 \text{ double Interest is} \\ \hline 12 \\ \text{Ans. } 1l. 5 \end{array} \quad \begin{array}{r} 05 * \\ \hline 125 \end{array}$$

EXAMPLE IX.

$$\begin{array}{r} \text{If it be required for } 6 \text{ and } \frac{1}{6}, \text{ Then } 12 \\ \hline 6 \\ \hline 12 \\ \text{And } \frac{1}{6} \text{ of } 2 \text{ will be found} \\ \hline 0125 \\ \text{And the Interest } 1l. 4s. 3d. \\ \hline 12125 \end{array}$$

EXAMPLE X.

WHAT is the Interest of 100000*l.* for 22 Days, at 3*l.* per Cent. per Annum.
(See Ex. 5. p. 22.)

• For 4 in 2 is 0, but a Cypher annext it goes 5 in 20:

The

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The Int. was found at 5 per Cent. 13|698620

Doub. and a Pl. more cut off for Pts. 173,726

Multiply by 3 the Rate into 22 Day *viz.* 66

$$\begin{array}{r} 16433356 \\ 16438356 \\ \hline 1801821916 \end{array}$$

Viz. 108L 16s. 5d. $\frac{5}{4}$

EXAMPLE XI.

WHAT is the Interest of 2156L 13s. 4d.
for 61 Days at 6L $\frac{3}{4}$ per Cent. per Ann.

The Principal doubled is 4313L 6s. 8d. (See
p. 26.)

The Int. of which for six Places is 59087
711

$$\begin{array}{r} 413609 \\ 147772 \\ \hline 398337 \\ 2392022 \\ \hline 2416s. 7d. Ans. for 61 Days 24|329057 \end{array}$$

As the Rate is first to be multiply'd by 1,
it is next multiply'd by 6, (as in Multiplication)
and added thereto.

As multiplying by 13, 14, 15, 16, 17, 18,
and 19, &c. in one Line (which is taught in
most Books of Arithmetic) will agreeably
shorten the Work, I shall here give the Me-
thod for those who have not seen it, &c.

|| Which is $\frac{1}{4}$ too much, $\frac{1}{4}$ of the Interest of the Day is
therefore taken from the Product.

After

After the first Figure in the Product is set down to the Multiplication of the second Figure in the Multiplicand, (with the Carriage from the former if any) you must add the next Right-hand Figure, setting down for the Product as usual, Proceeding so through the whole Multiplicand, to the Left-Hand of which it will be best for Beginners to suppose a Cypher for Conveniency, as will appear in the Examples.

E X A M P L E I.

WHAT is the Product of 3764 by 13, in one Line?

$$\begin{array}{r}
 3764 \\
 \times 13 \\
 \hline
 48932
 \end{array}$$

Here first 3 Times 4 is 12, *viz.* 2 and go 1; next 3 times 6 is 18 and 1 is 19, and 4 to the Right Hand is 23, *viz.* 3 and go 2. Again, 3 times 7 is 21 and 2 is 23, with 6 to the right Hand is 29, *viz.* 9 and go 2, also 3 times 3 is 9 and 2 is 11, with 7 to the right Hand is 18, *viz.* 8 and go 1. *Lastly,* supposing 0, 3 times 0 is 0, and 1 that was carried is 1, and 3 in this Case to the right Hand is 4, which set down gives the Product as above the like with all others.

Here

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Here it may be observ'd, that the last Carriage added to the last left Hand Figure in the Multiplicand, gives the last left Hand Figure &c. in the Product; whence the Supposition of an o may be omitted.

$$\begin{array}{r}
 625 \\
 16 \\
 \hline
 10000
 \end{array}
 \qquad
 \begin{array}{r}
 4793 \\
 19 \\
 \hline
 91067
 \end{array}$$

This may be done with 21, &c. to 29 taking in the double of the left Hand Figure in the Multiplicand; as also by 31, 42, and so thro' the nine Digits, taking in the Treble, Quadruple, &c.

E X A M P L E S.

$$\begin{array}{r}
 3764 \\
 23 \\
 \hline
 86572
 \end{array}
 \qquad
 \begin{array}{r}
 4625 \\
 34 \\
 \hline
 157250
 \end{array}
 \qquad
 \begin{array}{r}
 4793 \\
 46 \\
 \hline
 220478
 \end{array}$$

Or when the last Place to the right Hand of the Multiplier is Unity, after setting the said last Place (by 1) in the Product begin with the preceding Digit in the Multiplier taking in the next left Hand Place in the Multiplicand, and so on: Thus 3764 by 31.* First, once 4 is 4; next, 3 times 4 is 12 and 7 is 19, that is 9 and go 1; then 3 times 7 is 21 and 6 is 27, that is 7 and go 2: Again, 3 times 6 is 18 and 2 is 20 and 3 is 23, that is 3 and go 2.

Lastly,

* Which put down on Paper.

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Lastly, 3 times 3 is 9 and 2 is 11, which set in the Product as it is the last, gives 113894 the Answer. (Example 11, p. 29. may be thus wrought.)

To abridge in multiplying by 101 and so to 109 included.

Multiply by the single right Hand Digit, setting the Product two Places farther to the right Hand under the Multiplicand, which added thereto gives the Answer required.

Thus 3624 by 103 will be 3624

$$\begin{array}{r} 10872 \\ \hline 373272 \end{array}$$

To abridge in multiplying by 110.

Multiply by 11 in one Line (See p. 34) annexing a Cypher to the last right hand Place of the Product.

E X A M P L E.

$$\begin{array}{r} 3624 \\ \times 110 \\ \hline 398640 \end{array}$$

To abridge in multiplying by 111, 112, to 119 included.

Multiply by the two last right Hand Places in one Line, setting the Product two Places to the right Hand of the Multiplicand, and adding as before.

E X A M-

E X A M P L E III.

$$\begin{array}{r} 3624 \quad \text{by } 112 \\ 43488 \\ \hline 405888 \end{array}$$

To abridge in multiplying by † 120, 121,
and so to 199 included.

Multiply by the last right Hand Digit
next by the two preceding in one Line, set-
ting down as in other Multiplications.

E X A M P L E IV,

$$\begin{array}{r} 3624 \quad \text{by } 128 \\ 128 \\ \hline 28992 \\ 43488 \\ \hline 463872 \end{array}$$

It sometimes happens when Multipliers
consist of three or more Figures, that the
two next preceding the Digit you at any time
multiply by, is exactly divisible by the said
Digit, in which Case after multiplying by
that Digit multiply that Product by the
Quote or Number of Times the said two
preceding Digits contain, the other which
set down as in other Multiplications makes
the Process a Line less.

† This as by 110, p. 36.

EXAMPLE V.

LET $\begin{array}{r} 3624 \\ \times 8 \\ \hline 28992 \end{array}$ be multiplied by 328
 $\begin{array}{r} 115968 \\ \hline 1188672 \end{array}$ which mult. by 4 as under

This may be done in any Part of any Multiplier when it so happens.

It might also have been done multiplying by 28 in one Line, and next by 3, &c.

To multiply by 101 to 109 inclusive in one Line.

In multiplying by the first Digit when you come to the Place of Hundreds in the Multiplicand add to that Product the Unit's Place of the said Multiplicand, when to the Place of Thousands add the Place of Tens, and so on successively with the next Place till finish'd, when it will be best for Beginners to suppose two Cyphers to the Left of the Multiplicand, (as one before p. 34.)

Let 3624 be multiplied by 103.

$$\begin{array}{r} 103 \\ \times 3624 \\ \hline 373272 \end{array}$$

Here first 3 times 4 is 12, viz. 2 and go 1. Secondly, 3 times 2 is 6 and 1 is 7. Thirdly,

Thirdly, 3 times 6 is 18 and 4 in the Unit's Place of the Multiplicand is 22, *viz.* 2 and go 2. Fourthly, 3 times 3 is 9 and 2 carry'd is 11, and 2 in the Place of Tens is 13, *viz.* 3 and go 1; next, 3 times 0 is 0, but 1 and 6 in the Place of Hundreds is 7. Lastly, 3 times 0 is 0, but 3 the last Figure in the Multiplicand being set down gives the Product as before.

To multiply by 111 to 200, &c. in one Line.

Multiply by the two last right Hand Places by p. 34. taking in the Multiplicand as *per* last.

Let 3624 be multiplied by 119.

$$\begin{array}{r} \underline{119} \\ 431256 \end{array}$$

the like with others.

When the Place of Hundreds in the Multiplier is 2, 3, &c. you must take in twice, three times, &c. the proper Figures in the Multiplicand, by which means you may multiply by any three Figures.

From hence may be deduc'd the Method of multiplying by many more Figures in one Line; but when the Digits run high, even in three Figures, it is apt to crowd and load the Memory; when ever this happens it ceases to be useful, and of no other Advantage than saving a little Paper: Therefore,

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tho' by some one of the foregoing Contractions (as shall be found convenient) a Line more, &c. may be introduc'd; yet it will be found less irksome, more certain, and upon the Whole more expeditious.

The Method of valuing for Farthings (*See p. 5.*) is not the exact, (though near enough for Practice) but those who would be quite so may make use of the following Method, *viz.* multiply the Expression to the first Place for Farthings included by 4, setting the Product under two Places farther to the right Hand, next subtracting it therefrom gives the exact Answer required.

E X A M P L E I.

Take the Expression for Farthings to Example viii. *p. 12,* *viz.* $29942 \frac{1}{4}$

$$\begin{array}{r} 119768 \\ \hline 2874432 \end{array}$$

Here the true Value is 28 Farthings, 7 Tenths, or 74 Hundredths, or 744 Thousandths, or 7443 Ten Thousandths, or 7443^2 Hundred Thousandth Parts of a Farthing, which last subtracted from a Hundred Thousand, *viz.* 100000

Gives — $\frac{7443^2}{25568}$ so that the Value * estimated

† When the Skillings are valued. * In Page 12.

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mated is not three Tenth^s of a Farthing too
much, which is inconsiderable.

E X A M P L E II.

TAKE the Expression for Farthings to Ex-
ample ix. p. 32, *viz.* — 125

Here they are just 12 as estimated 500
12000

E X A M P L E III.

TAKE the Expression against 73 in the
second Part of the Table, *viz.* 101 here
a Cypher put to the right Hand (*See p. 13.*)
it becomes 10 for Farthings, or 2 d. $\frac{1}{2}$,
which is not exact, a proportional Part of 10,
viz. 25th Part thereof requiring to be de-
ducted, proceed therefore as in *p. 40,* (*viz.*)

010

40 Product by 4

00960 gives 9 Farthings and 6
Tenths of a Farthing, the true Answer re-
quired, the former Value being 4 Tenths of
a Farthing too much.

Against 365 is 105, which is just 5 times
that against 73 taken out as before, which 105
is in Value one Shilling or 48 Farthings;
(*See p. 6.*) therefore multiplying 0096 found
as above by 5, it gives 048, *viz.* 48 Far-
things, or one Shilling as before. It may
likewise

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likewise be observ'd, that as $\frac{1}{105}$ expresses the Interest of 365 £. for one Day, so it does also the Interest of 1 £. for 365 Days, or a Year, and in Part first $904\frac{1}{7}$ with two Cyphers suppos'd prefixt is the Interest of 1 £. for 66 Days, as well as of 66 £. for one Day the like with the rest.

To find the Parts that shall express the Value of Shillings, Pence and Farthings.

It is very easy for Shillings, which if even Half the Number will be the first Place of the Parts to the left Hand. Thus if 4 be the Shillings given, 2 will be the first Place of Parts. See *Ex. iii. p. 28,* and Observation thereon.

If the Shillings be odd annex or suppose a Cypher to the right Hand, Half of which will be the Expression required.

Thus if the Shillings be 7 , annexing a Cypher it gives 70 , the Half of which is 35 , for Answer, see *p. 5. Ex. i.* the like with all others.

Hence $\frac{1}{105}$ is the Expression for one Shilling as against 365 in the second Part of the Table (*See p. 41.*) for per the Rule a Cypher annexed to 1 makes 10 , when the Half of 1 is 0 , and of $10, 5, \text{ viz. } \frac{1}{105}, \text{ &c.}$

For Pence and Farthings.

Reduce the Pence to Farthings, and add the other Farthings if any thereto; next mul-

ply

ply by 4, adding as you multiply a * sixth Part of the said Farths. setting the Product under them two Places farther to the right Hand, their Sum gives the Expression required; observing, that when the Farthings consist but of one Place as 9, or under, two Cyphers must be prefixt thereto, but when of two Places (which is the most) one Cypher only.

When the Farthings are exactly divisible by 6, this will be the true Answer; and otherwise so extreamly near, as to be sufficient for almost any Purpose. But to be quite nice; add to the Remainder in taking the 6th Part of the Farthings an o, &c. (See Ex. 5. p. 30.) and divide by 6, setting the Quotient to the right Hand of the Expression found as before, which will then be the true Answer required.

E X A M P L E I.

WHAT is the Expression for 3 d. or 12 Farthings.—First, 4 times 2 is 8 and 2 for the 6th Part of the Farthings is 10, viz. 0 and go 1; next 4 times 1 is 4 and 1 is 5, which Product 50 placed after 12, as it is per the Rule, to be set two Places to the

* If the Remainder be 3 or upward make the Quotient one more, otherwise not.

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the right Hand, gives with the * Cypher prefixt 01250 which last Cypher to the right Hand omitted, gives the true Expression 0125 required.

E X A M P L E II.

W H A T is the Expression for 7 d. $\frac{1}{5}$, or 30 Farthings.

$$\begin{array}{r} 125 \text{ Product by 4, &c.} \\ \hline 03125 \text{ Expression required.} \end{array}$$

These Expressions are the true, as nothing remained in taking the 6th Part of the Farthings.

E X A M P L E III.

W H A T is the Expression for 4 d. or 16 Farthings. 16

$$\begin{array}{r} 67 \\ \hline 01667 \text{ Answer.} \end{array}$$

Here as 4 remained, the last Place to the right Hand in the Prod. by 4 is made one more.

* See Page 43.

E X.

EXAMPLE IV.

WHAT is the Expression for 2d. or
8 Farthings.

$$\begin{array}{r} 33 \\ \hline 100833 \end{array}$$

Answer.

Here the Remainder 2 after taking the 6th Part of the Farthings, gives *per* the Rule no Augmentation for the Product.

These two last Examples being not the precise or exact Expressions, it will be the best here to repeat the Work; observing the Rule for obtaining them:

Thus (Ex. iii) — 1016

$$\begin{array}{r} 66 \text{ mult. by } 4, \&c. \\ \hline 101666 \end{array}$$

first Expression.

Next as 4 remained in taking a 6th Part of the Farthings, by annexing 0 to the right Hand thereof it becomes 40, and dividing by 6, it gives 6 to be annexed to the right Hand of the Expression above found; and so proceeding on there will be a continual Repetition of 6; when this happens (as also with any other Digit) make a Dot over the first of them to the left Hand to distinguish it for that Purpose,

When.

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When the same will be contracted to |016
And the other to ————— |0083

Which Dots shew they may be continued on at Pleasure, and are the true Expressions.

The Rule for working with these repeating Digits is very easy, *viz.* When multiply'd by any other Digit you must add so many Units to that Product as are the Number of Nines in it, setting down the Digit dotted arising from this, as in the Product of other Multiplications.

E X A M P L E V.

WHAT is the Value of the Expression for Farthings, *viz.* 016 as above.

Thus |016 *

$$\begin{array}{r} 66 \\ \hline 1016 \end{array} \dagger$$

* Multiplying by 4, &c. setting the Product by Rule,
Page 33.

† Here as 6 in the Expression repeats it is to be continued out, or suppos'd so, till even with the under repeating 6, when subtracting the Repetition will be taken off, leaving 16 Farthings as at first.

For

For a farther Proof hereof let $101\dot{6}$ be
 multiply'd by 365

$$\begin{array}{r}
 & 365 \\
 \times & 101\dot{6} \\
 \hline
 & 83 \\
 & 100 \\
 & 50 \\
 \hline
 & 6|083
 \end{array}$$

Here as there are three Places in the Expression, there must be three in the Product, and the Value *per Rule* aforegoing, will be $6l. 1s.$, and $3\dot{3}$ for Farths next $|33$.

Making the Ans. $6l. 1s. 8d.$ $\underline{32}$ remaining Farthings or $8d.$

For as the 16 Farthings at first is $4d.$ therefore 365 Groats is 121 Shillings and $8,$ or $6l. 1s. 8d.$ as before.

EXAMPLE VI.

AGAIN let the same Expression, viz. $101\dot{6}$ be multiply'd by 241 .

$$\begin{array}{r}
 & 241 \\
 \times & 101\dot{6} \\
 \hline
 & 666 \\
 & 666 \\
 & 3333 \\
 \hline
 & 4|016
 \end{array}$$

Here

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Here as the dotted Figures in the several Products repeat—they are all except the first continued out till made even with the said . . First ————— next adding up that Line there is an Unit added to the Sum for the nine contained therein, making it 16, when setting down the 6 dotted, as it will repeat the true Product will be found as above, *viz.* 4*l.* and the Expression 1008 $\dot{3}$ to be 4*d.* which is plain, it being the same as at first, &c.

E X A M P L E VI.

LET the Expression 1008 $\dot{3}$ be multiply'd by 24*l.*

$$\begin{array}{r} 241 \\ \hline 83 \\ 333 \\ 166 \\ \hline 2 | 0083 \end{array}$$

333 mult. 4 &c.
008... *viz.* 8 Far-

things or 2*d.*

True Product 2*l.* os. 2*d.* the Half of the above, &c.

Here the dotted Digits in the several Products are not produc'd but suppos'd, which is very easy.

In

INTEREST Improved. 49

In finding the Expression for Pence and Farthings, no other Digit will be found to repeat but 3, or 6; whence these Examples are sufficient on that Head.

EXAMPLE VIII.

WHAT is the Expression for 9 d. $\frac{3}{4}$, or 39 Farthings.

$$\begin{array}{r} 162 \text{ by } 4, \&c. \\ \hline 040625 \end{array}$$

Here as 3 remained, by adding an o and dividing by 6 it gave 5, which annexing to the right Hand, gives 040625 the true Expression as nothing remained afterwards; which let be prov'd back for its Value in Farthings,

Viz.
$$\begin{array}{r} 040625 \\ 162500 \\ \hline 039 \dots \text{ Farthings as before.} \end{array}$$

Thus from what has been said, the true Expressions at any time may be found, as it were by Inspection, and any Number of those Places may be taken at Pleasure, as the Nature of the Case requires.

F

E X-

50 *INTEREST* Improved.

E X A M P L E IX.

W H A T is the Expression for 16 Shillings and 2d $\frac{1}{4}$.

For 16s. per foregoing, it is	8 *
For 9 Farthings <i>ditto</i>	— 009375
	———— 809375 Ans.

E X A M P L E X.

W H A T is the Expres. for 17s. 11d.

For 17s. it is	— 85
For 11d.	— 04583
	———— 89583 Ans.

E X A M P L E XI.

W H A T is the Expres. for 1s. & $\frac{1}{4}$.

For 1s. it is	— 05
For $\frac{1}{4}$ <i>ditto</i>	— 0010416
	———— 0510416 Ans.

Thus with extreme Ease may the true Expressions be found in all Cases.

And each of them in most Cases may be contracted. For in these Examples 8094, or 81 may be taken for the first, 8958, or 896 for

* The 1st Place to the left Hand.

I N T E R E S T Improved. 51

for the second; and 051 for the last, and that without any significant Error.

If these are valued by the common Rule of bating 1 for every 25, &c. then 051 will be 49 Farthings, or 1 s. & $\frac{1}{4}$, and 8958 will be 17 s., and by the * Rule the Remainder must be taken 46, and bating 2 becomes 44 Farthings, &c.

Any yearly Sum given to find per Table, what that is per Day.

If it be under 73*l.* take out the Interest of double the Sum (or double the Interest of the Sum) next cut off or separate from the Parts the last left Hand Place, the remaining Figures to the right Hand express the Value of the Money.

E X A M P L E I.

AT 54*l.* 15*s.* per Ann. what is that per Day.

Double <i>ditto</i>	109 <i>l.</i> 10
Next less in Tab.	<u>73</u> against it 10 <i>l.</i>
remaining	<u>36</u> 10 <i>ditto</i> <u>005‡</u> <u>015 </u>

F 2

E X-

* See Page 6.

‡ Which might at first have been placed after 01.
See p. 14. || Sum with the left Hand place separated, viz.
Three Shillings.

EXAMPLE II.

AT 45*l.* per *Ann.* what is that *per Day*.

Double *ditto* is 90*l.* and the Interest, &c. per foregoing of 12329 *viz.* 2*s.* 5*d.* $\frac{1}{2}$, &c.

If you would be more exact as to the Parts of a Farthing, multiply the Expression for Farthings, as directed in p. 40.

$$\begin{array}{r} \text{Viz.} & 2329 \\ & 9316 \\ \hline \text{Farthings} & 22\mid 3584 \end{array}$$

Which is 22 Farthings, 3 Tenth, or 35 Hundredths; or in the Whole 358 $\frac{4}{5}$ Ten Thousandth Parts of a Farthing more *per Day* than 2*s.* 5*d.* $\frac{1}{2}$. If the said Parts of a Farthing be multiply'd by 365.

$$\begin{array}{r} \text{Viz.} - & 3584 \\ & 365 \\ \hline & 17920 \\ & 21504 \\ & 10752 \\ \hline * & 130\mid 8160 \end{array}$$

If

* That is 130 Farthings, or 2*s.* 8*d.* more in the Year, which may be easily proved.

I N T E R E S T Improved. 53

If the same be required for any Number of Days of the Year, suppose 137 multiplying the Expression for one Day thereby gives the Answer required,

Thus

$$\begin{array}{r}
 12329 \\
 \times 137 \\
 \hline
 86303 \\
 160277 \\
 \hline
 * 16 | 89073
 \end{array}$$

If the said Expression for a Day be multiplied by 365 it will produce 45 the Pounds *per Annum.*

Thus.

$$\begin{array}{r}
 12329 \\
 \times 365 \\
 \hline
 61645 \\
 73974 \\
 36987 \\
 \hline
 45 | 00085
 \end{array}$$

The last 85 to the right Hand is here of no Value, the first Expression being not quite perfect, though near enough in all Reason.

From whence it may likewise be observ'd, that 12329 is also the Expression for 45 Days of a Year: So that taking at any Time the Days of a Year as *ls.* and proceeding ac-

F 3 cordingly,

* *Viz.* 16 l. 17 s. 9 d. $\frac{1}{2}$, &c.

54 *INTEREST* Improved.

cordingly; you will have the Expression for the said Number of Days required.

* If the yearly Sum be 73*l.* or upward: Take out the Interest of the said Sum from the Table, next double the said Interest proceeding in other Respects as before.

E X A M P L E III.

AT 744*l.* 16*s.* 9*d.* per Annum, What is that *per Day*.

The Int. from Tab. will be found 102033
Multiply by 2
Viz. 2*l.* 0*s.* 9*d.* $\frac{3}{4}$ *per Day* 2|04066

E X A M P L E IV.

AT 4088*l.* 8*s.* 7*d.* per Annum, What is that *per Day*.

Interest, &c. will be found 560058
Double 1|120116

But *per* the Rule when the last left Hand Place of Parts is separated it will become 11|20116, viz. 11*l.* 4*s.* 0*d.* $\frac{1}{4}$ *per Day*.

E X-

* Though this may be done by the foregoing Method, and that by this, yet each as us'd, will be found to have its Conveniency.

E X A M P L E V.

AT $7300l.$ per Annum, What is that per Day.

The Interest is 1, an Integer, which doubled is 2; next seeing there are no Places of Parts, * Cyphers must be supposed to the right Hand, and one separated to the left when it will become 20, *viz.* $20l.$ per Diem. See Ex. 3. p. 20.

If the Annuity be more than $7300l.$ the greatest in the Table, divide the said Annuity thereby, when the Quote will be so many times $20l.$ next seek for the Remainder by Rules aforesaid.

E X A M P L E VI.

AT $44327l.$ $14s.$ $9d.$ per Annum, What is that per Day.

The Pounds divided by 7300 gives 6 for the Quote, and $527l.$ $14\frac{9}{12}d.$ Remainder, the Interest for which doubled will be found $1|44586$, which added to 120 (*viz.* 6 times 20) gives $121l.$ $8s.$ $11d.$ Answer the like with all others.

Any daily Sum, given to find what that is per Annum.

Find the Expression for half the given Sum;

* See Ex. 3d. p. 20.

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Sum; (See p. 42.) (or for the Whole, and take the Half, but the first is generally most convenient) next prefix a Cypher to the left Hand thereof, the Principal answering to this in the Table gives the Answer.

E X A M P L E I.

AT 3*s.* per Day, What is that *per Annum.*

The Expression for 1*s.* 6*d.* (See p. 35) is 075, and a Cypher prefixt by the Precept is 0075, which must be sought for among the Interests in that Part of the Table, where two Cyphers are suppos'd prefixt, which falls in the last Column of Part the first.

Thus Express. 1st found is 0075.. ||

* 7397 †

Remainder 000103 ‡

Making for Answer 54*l.* 15*s.*

|| Two Cyphers supposed for six Places.

† Next less in Table (with two Cyphers suppos'd.

I † And against it 54*l.* 00 Principal.

‡ Ditto - - 103 15 0

E X A M-

E X A M P L E II.

AT 17*s.* 9*d.* *per Day*, What is that *per Annum*.

Exp. for 8*s.* 10*d.* $\frac{1}{2}$ *&c.* is 1044375

In 2d Part Tab. against 104.... is 292*l.*

Rem. 1004375

Int. *dit.* with 2 Cyph. sup. 4247 is 31*l.* 0

Rem. 128

Ditto 3 Cyph. sup. 123 is 18*s.*

$\frac{123}{*5}$

Making the Answer 323*l.* 18*s.* 9*d.*

E X A M P L E III.

TH E Expression *per Day* for 45*l.* *per Annum* found as before was + 12329 the Half ordered by the \ddagger Rule will be 006164, against which in the Table, Part I, where two Cyphers are suppos'd is 45, which prov'd the Rule.

Hence it is obvious as 12329 was also the Expression for 45 Days of a Year. That any other Expression ordered *per* the Rule, the Number of Days answering thereto may likewise be found, it being the same with the Pounds.

If

* And against 5, *viz.* 3 and 2 are 5*d.* and 4*d.* *viz.* 9*d.*

\ddagger See p. 52.

\ddagger See p. 55, 56.

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If Half the daily Sum consists of Pounds, Shillings, &c. find the Expression for the Shillings, &c. next instead of prefixing a Cypher thereto, seperate the Units Place of half the Sum from the Pounds to the Parts, which will then be the Expression required, (and is the Converse to Exp. 4. p. 54.)

E X A M P L E IV.

AT $2l. 4\circ$ per Day, What is that *per Annum*.

The Half is $1l. 2$, and the Expression for $2s.$ is $|1$ next (instead of a Cypher) prefixing the $1l.$ it becomes $|11.$ Against which in Table, Part II. Answ^r $803l.$ and is so much *per Annum*.

E X.

E X A M P L E V.

AT 3*l.* 13*s.* 6*d.* per Day, what is that
per Annum.

The Half is 1*l.* 16*s.* 9*d.* the Expression
for which is |8375.

And the 1 prefixt makes |18375

In the Tab. against 18 ... is 1314*l.*

Remainder .. 375
In Tab. against ————— 3699 is 27*l.*

Remainder 51
In Tab. against ————— 48 is 7*s.*

Remainder *3
against 2 & 1. viz. 3 the Rem. is 4*d* & 2d viz. 6*d*

Answer 1341 l 7s 6d

* See p. 11.

EXAMPLE VI.

AT $21l. 50$ per Day, What is that *per Annum.*

The Half is $10l. 12\frac{1}{2}$, the Expression for $12s. 6d.$ is 625 , to which as the Units Place of half the Sum, *viz.* $10l.$ is possest by an o , the same must be prefixt,

Making	-	$1 0625$
	+	<u>1</u> is $7300l.$
		Remainder 0625
In Tab. against	<u>—</u>	<u>06..</u> is $438\ 0\ 0$
		Remainder $..25$
In Tab. against	<u>—</u>	<u>..2466</u> is $18\ 0\ 0$
In Tab. against	<u>—</u>	<u>....34</u> is $0\ 5\ 0$
Making the Answer		<u>7756 5 0</u>

If the daily Sum be great, it may be done *per* the Converse to Example 6. p. 55, suppose $154l.$ *per Day*, which ordered will be $7|7$. Then 7 times 7300 is 51100 , and against 7 is 5110 , making $56210l.$ Answer. By a little Application all this will be very familiar, and done as it were at Sight.

The foregoing Examples amply explain the Use of the Table, in finding at all Rates the Interest of any Principal for Days. But for

† Next in the Table against 1, which is here Integral.

INTEREST Improved. 61
for entire Years, the following Examples exhibit a very easy and concise Method.

R U L E.

WHEN the Principal consists of two or more Integral Places, multiply the same by the \dagger Rate, and this Product by the Number of Years; next separate from this last Product two Integral Places to the right Hand for Parts, which gives the Answer required.

E X A M P L E I.

WHAT is the Interest of 148*l.* for 3 Years at 5 per Cent. per Annum.

$$\begin{array}{r} 148 \\ \times 5 \\ \hline 740 \\ -3 \\ \hline 22\mid 20^* \end{array}$$

Or the two integral Places may be separated from the Principals at first for Parts, when multiplying by the Rule the Product will be the Answer, with two Places of Parts therein as before.

G

E X-

\dagger Which for Illustration is first taken Integral.

* Which is dividing by 100. See P. 28.

EXAMPLE VI.

AT $21l. 50$ per Day, What is that *per Annum.*

The Half is $10l. 12s. 6d.$, the Expression for $12s. 6d.$ is 625 , to which as the Units Place of half the Sum, *viz.* $10l.$ is possest by an o , the same must be prefixt,

Making	-	$1 0625$
	+	<u>1</u> is $7300l.$
		Remainder <u>0625</u>
In Tab. against	<u>—</u>	<u>06..</u> is $438\ 00$
		Remainder <u>..25</u>
In Tab. against	<u>—</u>	<u>..2466</u> is $18\ 00$
In Tab. against	<u>—</u>	<u>....34</u> is $0\ 50$
Making the Answer		<u>7756</u> <u>50</u>

If the daily Sum be great, it may be done *per* the Converse to Example 6. p. 55, suppose $154l.$ *per Day*, which ordered will be $7|7$. Then 7 times 7300 is 51100 , and against 7 is 5110 , making $56210l.$ Answer. By a little Application all this will be very familiar, and done as it were at Sight.

The foregoing Examples amply explain the Use of the Table, in finding at all Rates the Interest of any Principal for Days. But for

† Next in the Table against 1, which is here Integral.

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for entire Years, the following Examples exhibit a very easy and concise Method.

R U L E.

WHEN the Principal consists of two or more Integral Places, multiply the same by the \dagger Rate, and this Product by the Number of Years; next separate from this last Product two Integral Places to the right Hand for Parts, which gives the Answer required.

E X A M P L E I.

WHAT is the Interest of 148*l.* for 3 Years at 5 per Cent. per Annum.

$$\begin{array}{r} 148 \\ \times 5 \\ \hline 740 \\ -3 \\ \hline 22\mid 20^* \end{array}$$

Or the two integral Places may be separated from the Principals at first for Parts, when multiplying by the Rule the Product will be the Answer, with two Places of Parts therein as before.

G

E X-

\dagger Which for Illustration is first taken Integral.

* Which is dividing by 100. See P. 28.

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E X A M P L E II.

Thus —
$$\begin{array}{r} 1|48 + \\ 15 * \\ \hline 22|20 \end{array}$$

When the Principal consists but of two Integral Places, they may be both seperated at first for Parts, which multiply'd by the Rate and Time as before, they will be two Places for Parts in the Product.

E X A M P L E III.

W H A T is the Interest of 10*l.* for a Year at 1*l. per Cent. per Annum.*

Which is if 100*l.* give 1*l.* Interest for a Year, what will 10*l.* give. Which order'd accordingly, it will be 10 Parts or 2 Shillings. See p. 5.

When the Principal consists but of one Integral Place prefix a Cypher thereto, and separate both for Parts, &c.

E X A M P L E IV.

W H A T is the Interest of 1*l.* for a Year at 1*l. per Cent. per Annum.*

Which will become 101 Parts. See Observation,

† Which is the Interest for one Year at 1*l. per Cent.*

* Which is the Product of the Rate into the Time, and then multiplied in one Line. See p. 34.

vation, p. 28, and may be valued p. 40.

When the Principal consists of no Integral Places but all Parts prefix two Cyphers thereto, and separate all for Parts.

E X A M P L E V.

W H A T is the Interest of 12s. and 6d.
for a Year at 1*l.* per Cent. per Annum.

The Expression for 12s. 6d. is |625,
which will become |00625, *viz.* 1*d.* $\frac{1}{2}$. (See
p. 42.)

It is obvious in these four last Examples
that the Principal is divided by 100 to give
the Number of Parts for the Product, and
that it would have been equally the same if
the Product at last had been divided by 100;
from whence may be easily seen the Reason
of the following general

R U L E.

Multiply the Principal, Rate and Time as
per Rule the first; next separate two
Places more for Parts in the Product than are
in the said Principal, Rate and Time, pre-
fixing Cyphers to the Product when defi-
cient, which will then be the true Answer re-
quired.

EXAMPLE VII.

W H A T is the Interest of 13*s.* and 4*d.*
for a Year at 5 *per Cent. per Annum.*

$$\begin{array}{r} |6 * \\ 5 \text{ Rate} \\ \hline |033 \text{ or } 8d. \text{ See p. 47.} \end{array}$$

Here as there was but one Place of Parts in the Principal there required three in the Product, but as there was but two by the Multiplication a Cypher was prefix'd according to the Rule.

EXAMPLE VIII.

W H A T is the Interest of one Shilling
for a Year at 2*l. per Cent. per Ann.*

Express. for a Shil. is |05
 $\begin{array}{r} 2 \text{ Rate} \\ \hline |0010 \text{ viz. } \frac{1}{2} \text{ nearly.} \end{array}$

Here as there was two Places of Parts in the Principal there required four in the Product, and two Cyphers prefixt according to the Rule.

E X-

* The Expression for 13*s. 4d.* (See p. 42. and Ex. III. p. 44, also p. 46.)

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E X A M P L E IX.

WHAT is the Interest of 282*l.* 13*s.* 3*d.*
for 6 Years at 3*l.* 10*d.* per Cent. per
Annum.

Principal	282 6625
Rate	3 5
	—
	14133125
	8479875
	—
Years	98931875
	6
	—
	59 3591250 viz. 59 <i>l.</i> 7 <i>s.</i> 2 <i>d.</i> $\frac{3}{4}$.

Here as there are 5 Places of Parts in the Principal and Rate, there are required seven in the Product, which is separated accordingly.

But as the Rate into the Time gives 21 an Integral, the said Principal might have been multiply'd thereby in one Lines.

$$\begin{array}{r} \text{Thus} & 282|6625 \\ & 21 * \\ \hline & 59|359125 \end{array}$$

Or || two Integral Places might have been separated at first for Parts to the Four, which would have then been six for the Product.

G 3

E X-

* See p. 35, and Example II. p. 62.

|| See p. 61.

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E X A M P L E X.

WHAT is the Interest of 231*l.* 13*s.* 6*d.* $\frac{3}{4}$ at 4*l.* 1*s.* 3*d.* per Cent. per Annum for 5 Years.

Principal	231 678125
Rate	4 0625
	—————
	1158390625
	463356250
	1390068750
	926712500
	—————
	9411923828125
Numb. Years	5
	—————
	47 059619140625 Viz. 47 <i>l.</i>
1 <i>s.</i> 2 <i>d.</i> $\frac{3}{4}$ Answer.	

Here as there are six Places in the Principal, and four in the Rate, *viz.* Ten, there are Twelve separated in the Product, according to the Rule the like with all others.

But these Multiplications by all the Figures being very tedious; and as no more than four Places are ever necessary in the Product for securing the Value of the Money.

I shall next insert the Rule for that Purpose, which will greatly shorten and make easy the Work.

After two Places are separated from the Principal for Parts (to the rest if any) as before

fore * shewn, set the Figure in the Units Place of the Rate under the † fourth Place of Parts in the Product by the Time ; inverting every other Place of the Rate on the right Hand to the left, and on the left Hand to the right, when multiply as usual, beginning with that Place in the Principal, which is directly over the last right Hand Place of the inverted Rate taking in the Carriage of the next Digit (or two) to the right Hand, set the first Digit (or o) arising from this directly under the same, proceeding after as in other Multiplication.

Observe the same with the next multiplying Digit, beginning also at the Place directly over it, having Regard to the Carriage as before, the Digit (or o) here must be set directly under the last to the right Hand of the former Product, proceeding on as usual.

This Method being observ'd throughout ; the Addition of the several Products, will be that with four Places of Parts required. Observing in these Cases, first to multiply the Principal so ordered by the Time as follows. Take the last Example.

* P. 62.

† If it be required for three Places, it must be put under the third, the like for any other Number.

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Principal, &c.		2 31678125
Time	—	5
	—	11 58390625*
Rate inverted	—	5 2604
	—	463356
	—	6950
	—	232
	—	58

Viz. 47 l. 1 s. 2 d. $\frac{1}{4}$ as before 47|0596

Here in multiplying 8 by 6, the Carriage from the two right Hand Digits was 2, which made 50, &c.

Next by 2 the Carriage was 1 and above 6 Parts, but when it is 5 or upward, the Carriage may be made one more, which is therefore taken 2, and the rather, as there was some Defect in the Carriage before by 6.

In multiplying by 5, the Carriage was so extremely near 3, that it was taken as such.

This alternately observed, there will seldom or never be an Error in the fourth Place of Parts from that wrought at large, and if by

* Here it may be seen, that there was no Occasion of multiplying all the Figures of the Principal by the Time, but to have begun only at the fifth Place; the like of others with regard to the Carriage of the sixth.

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by Chance it should err an Unit, 'twill be of no Signification.

By this Method may the Interests by the Number of Days in the first Part of the Table, be greatly abridged in contracting for three Places, which will always be within half a Farthing.

Take Example I. p. 5. viz. 959

$$\begin{array}{r} 563 \\ \hline 288 \\ 57 \\ \hline 5 \\ \hline |350 \end{array}$$

Here you must observe, that as there are 3 Cyphers, supposed before 959, 5 in the Units Place of the Multiplier, is put under the 3d suppos'd Cypher, and the two other (Integral) Digits inverted to the right Hand, as per the Rule, p. 67.

Next in the multiplying by 3, the Carriage was taken a little too much; by 6, too little, and lastly, by 5 somewhat too much, all which is very obvious, so that the Defect in the Product will be always insignificant.

Take

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Take Example V. p. 8. viz. 3562

$$\begin{array}{r}
 782 \\
 - 712 \\
 \hline
 285 \\
 - 25 \\
 \hline
 1022
 \end{array}$$

By this Method may all the Examples be done, and to four Places, if three should not be thought sufficient, &c.

If at any Time the Rate of Interest should consist only of Parts, as it will when it is under 1*l. Sterling*.

You must Place a Cypher under that Place of Parts in the Product of the Principal into the Time, as you intend the Number of Places in the Product by the Rate; next invert, all to the left, and multiply as before.

Again, What is the Interest of the last Example p. 68. for the same Time at 2*s. 6d.* per Cent. with three Places of Parts in the Product or Answer.

Principal, &c. as before

$$\begin{array}{r}
 11|5839 \\
 521|0 \\
 \hline
 1158 \\
 232 \\
 58 \\
 \hline
 1|448
 \end{array}$$

Viz. 1*l. 8s. 11d. $\frac{1}{2}$*

Of

Of DISCOMPT.

THE customary Method (especially for Days) is to find the Interest of the Principal for the given Time, and to deduct it from the said Principal for the present Worth.

But the true Rule is to add to 1*l.* its Interest for the given Time, when it will be as the Sum of the said 1*l.* and its Interest is to 1*l.* so is the given Principal to its present Worth. Dividing therefore any Principal by the Sum of 1*l.* and its Interest for the given Time, the Quotient will be the present Worth required.

L E M M A.

IF two Numbers be multiplied by any Number, the Products divided one by the other, will give a Quotient equal to that of the two Numbers divided respectively one by the other.

Suppose 2 and 6, which let be multiplied by 10, the Products 20 and 60 divided as aforesaid, the Quotient 3, will be equal to 6 divided by 2, the like with any other Number, &c.

E X A M-

EXAMPLE I.

WHAT is the present Worth of 100*l.*
due a Year hence at 5*l.* per Cent. per
Annum?

The Interest of 1*l.* for a Year (*see p. 42.*) is 10*s.*, which added to 1, gives 110*s.*

Thus stated 105) 100 (But when the Divisor has Parts, and the Dividend is a whole Number, by annexing so many Cyphers to the right Hand of the Dividend, as there are Parts in the Divisor, (which is here multiplying both by 100, (*see Note, p. 20.* and the above *Lemma*,) you must then divide as in the whole Numbers, when the Quotient will be so far Integral (with Parts if divided farther on, *see p. 30, 31.*) and give the Answer required.

Thus * 105) 10000 (95| 238 viz. 95 l. 4 s. 9 d. $\frac{1}{4}$
 550 [nearly.
 250
 400
 850
 (10)

The Product of each Figure of the Divisor, with that of the Quotient, is taken from the Dividend (borrowing so many tens as are requisite)

* From whence you have also this Proportion, *viz.*
As 100*l.* with its Interest for the given Time is to 100,
 so is any Principal to its present Worth.

requisite) and the Remainder at the same Time only set down. Thus 9 times 5, *viz.* 45 from 50, the Remainder 5 is set down; next 9 times 0 is 0, with 5 that was borrowed is 5, from 10 leaves 5, which is also set down; lastly, 9 times 1 is 9, and 1 that was borrowed is 10, from 10 leaves no Remainder, the like with others.

But when the Principal and Divisor both consist of Parts, you must separate so many from the Principal to the left Hand, as there are in the said Divisor, when if the Parts in the said Principal falls short, you must annex a * Cypher or Cyphers as in *Example I.*

EXAMPLE II.

WHAT is the present Worth of 144*l.* 17*s.*
7*d.* due a Year hence at 5*l.* per Cent.
per Annum.

$$\begin{array}{r}
 \text{First Station } 105)144|87916 \\
 \text{Second ditto } 105)14487|916(137|980 \dagger \\
 \quad 398 \\
 \quad 837 \\
 \quad 1029 \\
 \quad 841 \\
 \quad (16)
 \end{array}$$

Hence it will be easy to prepare for your Division at one Station.

* But if any Digit in the Dividend should repeat, that must be continued on, as Occasion requires, see P. 46, &c.

† *Viz.* 137*l.* 19*s.* 7*d.* $\frac{1}{4}$.

EXAMPLE I.

WHAT is the present Worth of 100*l.* due a Year hence at 5*l.* per Cent. per Annum?

The Interest of 1*l.* for a Year (*see p. 42.*) is 10*s.*, which added to 1, gives 110*s.*

Thus stated 110*s.* 100 (But when the Divisor has Parts, and the Dividend is a whole Number, by annexing so many Cyphers to the right Hand of the Dividend, as there are Parts in the Divisor, (which is here multiplying both by 100, (*see Note, p. 20.* and the above *Lemma,*) you must then divide as in the whole Numbers, when the Quotient will be so far Integral (with Parts if divided farther on, *see p. 30, 31.*) and give the Answer required.

$$\begin{array}{r} \text{Thus } * 105) 10000 (95|238 \text{ viz. } 95\text{i}.4s.9d.\frac{1}{4} \\ 550 \\ 250 \\ 400 \\ 850 \\ (10) \end{array} \quad [\text{nearly.}]$$

The Product of each Figure of the Divisor, with that of the Quotient, is taken from the Dividend (borrowing so many tens as are requisite)

* From whence you have also this Proportion, *viz.* As 100*l.* with its Interest for the given Time is to 100, so is any Principal to its present Worth.

requisite) and the Remainder at the same Time only set down. Thus 9 times 5, *viz.* 45 from 50, the Remainder 5 is set down; next 9 times 0 is 0, with 5 that was borrowed is 5, from 10 leaves 5, which is also set down; lastly, 9 times 1 is 9, and 1 that was borrowed is 10, from 10 leaves no Remainder, the like with others.

But when the Principal and Divisor both consist of Parts, you must separate so many from the Principal to the left Hand, as there are in the said Divisor, when if the Parts in the said Principal falls short, you must annex a * Cypher or Cyphers as in *Example I.*

E X A M P L E II.

WHAT is the present Worth of 144*l.* 17*s.* 7*d.* due a Year hence at 5*l.* per Cent. *per Annum.*

$$\begin{array}{r}
 \text{First Station } 105)144|87916 \\
 \text{Second ditto } 105)14487|916(137|980 \dagger \\
 \quad\quad\quad 398 \\
 \quad\quad\quad 837 \\
 \quad\quad\quad 1029 \\
 \quad\quad\quad 841 \\
 \quad\quad\quad (16)
 \end{array}$$

Hence it will be easy to prepare for your Division at one Station.

* But if any Digit in the Dividend should repeat, that must be continued on, as Occasion requires, see P. 46, &c.

† *Viz.* 137*l.* 19*s.* 7*d.* $\frac{1}{4}$.

E X A M P L E III.

WHAT is the present Worth of 1*l.* due
a Year hence, at 5*l.* per Cent. per Ann.

Which stated according to the Rule is
105)100|0 (|95238 viz. 19 s. 0 d. $\frac{1}{2}$, &c.
which will then be us follows;

$$\begin{array}{r}
 105)100|0 (|95238 \text{ viz. } 19 \text{ s. } 0 \text{ d. } \frac{1}{2}, \& c. \\
 550 \\
 253 \\
 400 \\
 850 \\
 10
 \end{array}$$

From *Example I.* it is seen that by taking
the Interest of 100*l.* for a Year therefrom,
according to the customary Method, is taking
4*s.* 9*d.* and nearly $\frac{1}{4}$ too much.

And from *Exam. II.* it will be found nearly
7*s.* too much.

Proceeding according to these Rules with
any other Rate, which is very easily found
from *Rule p. 23 and 24, &c.* you wil have
the Answer accordingly.

EX AM-

E X A M P L E IV.

WHAT is the present Worth of 193*l.*
13*s.* 10*d.* due five Years hence, at
4*l.* 10*s.* per Cent. per Annum.

Rate at 5 per Ct.	05	Given Prin. 193 6916.
Double ditto requ.	9	
Rate ditto	045	
Years	— 5	
Int. for 5 Years	225	
Ad.to 1 <i>l.</i> &c. is 1	225	

Stated per foreg. 1225)193691|*6(158|1156†

7119
9941
1416
1916
6916
7916
&c.

After this Manner you may proceed with any Principal and Rate required.

* As 6 the last Figure in the Dividend repeated, it was brought down to the respective Remainders.

† Viz. 158*l.* 2*s.* 3*d.* $\frac{3}{4}$.

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	<i>l.</i>	<i>s.</i>	<i>d.</i>
The aforesaid Principal, —	193	13	10
Interest <i>ditto</i> for 5 Years deduct	43	11	7 $\frac{1}{4}$
Rem. accord. to custom. Meth.	150	2	2 $\frac{3}{4}$
But the present worth <i>per last</i> , is	158	2	3 $\frac{3}{4}$
Which is taking too much by	8	0	1

E X A M P L E V.

WHAT is the present worth of 193*l.*
13*s.* 10*d.* due 217 Days hence, at
4*l.* $\frac{1}{2}$ per Cent. per Annum.

Here (as in *P.* 42.) the Interest of 1*l.* for
217 Days, is the same as 217*l.* for one Day.
Therefore in the Table against 146 is 02, and
against 71, is 9726, *viz.* 029726 at 5*l.p.C.p.A.*

Double Rate 9

For 4 $\frac{1}{2}$ per Cent. 025753(4)

And *per fore.* 1025753)193691666(18818287
9111636
9056126
8501026
2950026
8985206
7791826
&c.

* See Note, page 73, 75.

Here

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Here the present Worth is 188*l.* 16*s.* 7*d.*
nearly.

	<i>l. s. d.</i>
Principal — —	193 13 10
Interest 217 Days deduct	5 3 7 $\frac{1}{2}$
Remains — —	188 10 2 $\frac{1}{2}$

Therefore according to the customary Way the Difference is 6*s.* 4*d.* $\frac{1}{2}$ in favour of the Discompter.

The Work of these Divisions may many Times be greatly contracted without any significant Error ; thus, instead of bringing down a Place or Figure from the Dividend, at each time cut one off from the Divisor, regarding only the Carriage (as in Multiplication, pag. 67.) to the Product, made by the Quotient Figure, and the next right Hand Place, or two, in the Divisor, and this done at every Operation throughout the Divisor, will give the Quotient required.

* Take the last Example.

$$\begin{array}{r}
 1]0|2|5|7|5|3)193691666(188|8288 \\
 911163 \\
 90561 \\
 8501 \\
 295 \\
 90 \\
 8 \\
 (0)
 \end{array}$$

In these Contractions it is requisite previously to determine the Value of the first Figure of the Quotient, as also how far it will be Integral and the like ; when in this Example it would have been till the two last right Hand Figures of the Dividend had been brought down, which at first Sight is found to be three Places.

Secondly, As both the Divisor and Dividend are made here Integral, and the Units Place of the Divisor, with the first Figure of Quotient fell under the third Place from the right Hand of the Dividend, the first Figure of the Quotient will therefore be of the same Value with it, *viz.* in the Place of Hundreds + which is obvious the like with others.

* Which will be best for Beginners to work this over again on Paper.

+ See Examples, pag. 20, &c.

Lastly,

Lastly, When the remaining Places of the Divisor will not go in those of the Dividend, a Cypher must be put in the Quotient, and another Place in the Divisor be cut off, and so on.

As four Places for Parts are found necessary to be in the Quotient, for securing the Value of Money, you must sometimes, before you begin the Contraction (when the Places of the Divisor are few) bring down some of the Places in the Dividend, by adding Cyphers when requisite, proceeding on as usual.

To illustrate which take Example 4th as follows :

$$\begin{array}{r} 1|2|2|5)193691|6(158|1156 \\ \quad 7119 \\ \quad 9941 \\ \quad 1416 \\ \quad 191 \\ \quad 68 \\ \quad 7 \\ (0) \end{array}$$

Here the Contraction did not begin till 191 remained, which in this Case (tho' it may in others) was scarce worth while, but for Illustration's Sake.

EXAMPLE VI.

WHAT is the present Worth of 6d. a Year hence at 5*l.* per Cent. per Ann.

Stated *per* Rules foregoing is

$$\begin{array}{r} 105)2\mid 50(0238 \text{ viz. } 23 \text{ Farthings nearly.} \\ 400 \\ 850 \\ (10) \end{array}$$

In this Example (*See Ex. 2d and 3d. p. 73, 74*) the Unit's Place of the Divisor into the first Figure of the Quotient fell under the second Place of Parts in the Dividend; the first Figure or Digit of the Quotient must therefore be of the same Value, and a Cypher placed before it for that * Purpose. If it had fell under the third Place of Parts two Cyphers must have been placed before it, and so on, which is the Reverse to Example *p. 20.*

What is a Security or Bond of 100*l.* at 4 per Cent. per Ann. payable a Year hence, worth at the Expiration of a Quarter of a Year?

In this Case the Principal when due will be 104*l.* next see how long it is before it comes due, which here is three Quarters of a Year;

* Hence appears the Reason in Ex. 5th and 6th, p. 30 and 31.

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then find the Interest at the Rate *per Cent.* for the said Time, which here is $3\frac{1}{2}l.$ the same added to 100 (See Note to Ex. 1. p. 72) is the Divisor, by which dividing the Principal into 100, gives the Answer required.

$$\begin{array}{r} \text{Thus } 103)10400(100|9708 \quad \text{viz. } 100l. \\ \qquad\qquad\qquad 1000 \qquad\qquad\qquad 19s. 5d. \\ \qquad\qquad\qquad 730 \\ \qquad\qquad\qquad 900 \\ \qquad\qquad\qquad 76 \\ \qquad\qquad\qquad \mathfrak{E}c. \end{array}$$

OF STOCKS.

EXAMPLE I.

SUPPOSE South-Sea or any Stock at $105\frac{3}{4}l.$ when the Half Year's Interest (which is $2\frac{1}{2}l.$) is paid off, what will it be worth 87 Days before the next Half Year's Interest becomes due, on that Consideration only?

$$\begin{array}{r} \text{Int. of } 87l. \text{ (See p. 42.) by Table} \\ \text{a } 15l. \text{ per Cent.} \quad \underline{\quad} \quad \underline{\quad} \quad 011918 \\ \text{Double Rate required (See p. 23.)} \quad \underline{\quad} \quad 8 \\ \qquad\qquad\qquad 009534\frac{1}{4} \end{array}$$

First

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First State (*See p. 73.*) 1|009534)107|375

$$\begin{array}{r} \text{2d ditto } 1|0|0|9|5|3|4)107375000(106|3609 \\ & \quad 64216 \\ & \quad 3644 \\ & \quad 615 \\ & \quad \quad 9 \\ & \quad \quad (0) \end{array}$$

Giving for Answer 106*l.* 7*s.* 2*d.* nearly.

Here it may be observed, that at the first Remainder of five Places, the 4 being cut off from the Divisor, the remaining 6 Places would not go in the said Remainder, a Cypher therefore was put in the Quotient, and the 3 cut off according to the Rule; the same was done at 9 the Remainder; the like with others.

It was likewise plain at first (*See p. 78.*) that the Quotient would contain three Places for whole Numbers, and that, contracting the Division, there would be four Places for Parts therein.

E X A M P L E II.

WHEN Stock is at 4*l. per Cent.* and 114*l.* is paid for 100*l.* Stock, what is that *per Cent.* That is, as 114 is to 100, so is 4 to the Answer. Or,

The

pai
31

INTEREST Improved. 83

The State of the Question may be, If 114*l.* get 4*l.* per Annum, what will 100*l.* get?

$$\begin{array}{r} 114)400(3]5088 \text{ viz. } 3l. 10s. 2d. \\ 580 \\ 1000 \\ 880 \\ \mathcal{E}c. \end{array}$$

EXAMPLE III.

IF there be paid 3*l.* 10*s.* per Annum for 100*l.* Stock, and there should after be allowed 4*l.* per Annum for the same, what would 100*l.* be worth upon that Rise of Interest?

Viz. As 3|5 is to 4, so is 100*l.* to the Answer.

Stated by Rule aforesaid

$$\begin{array}{r} 35)4000(114|2857 \text{ viz. } 114l. 3s. 8d. \frac{3}{2} \\ 50 \\ 150 \\ 100 \\ 300 \\ 200 \\ 250 \\ \mathcal{E}c. \end{array}$$

If when Stock is at 112*l.* there be 4*l.* per C_{t.} paid, what would it be worth if reduced to 3 per Cent.

As

84 *INTEREST Improved.*

As 4 to 112, so is 3 to the Answer,
viz. 84, &c.

E X A M P L E IV.

IF 100*l.* Stock be bought for $93\frac{1}{2}$ for which is paid 4*l.* Interest *per Annum*, what is that *per Cent.*

As $93\frac{1}{2}$ is to 100, so is 4 to the Answer.

$$\begin{array}{r}
 935)4000(4|2780 \text{ viz. } 4l. 3s. 6d. \frac{3}{4} \\
 2600 \\
 7300 \\
 7550 \\
 70 \\
 \&c.
 \end{array}$$

E X A M P L E V.

IF 100*l.* Stock be bought for $93\frac{3}{8}l.$ (viz. $93l. 7s. 6d.$) for which is paid 4*l.* Interest *per Annum*, what is that *per Cent.*

Stated, &c. 9|3|3|7|5)400000)4|2838 *viz.* 4*l.*

26500	[5s. 8d. p.Ct.
7825	
355	
75	
(0)	

Here it is to be observed, that the Product of the Division of the first Figure of the Quo-

INTEREST Improved. 85

Quotient took up all the Places of the Dividend, so that there could be no more Integrals in the Quotient ; next it is also as easily observed, that by contracting there would then be 4 Places of Parts, for the Quotient, &c.

EXAMPLE VI.

If a Blank Lottery Ticket, or Annuity, of 6*l.* be sold for 5*l.* 7*s.* 6*d.* what will a Blank of 100*l.* be worth at that Rate?

That is, as 6 is to 5|375, so is 100 to the Answer.

Thus 6)†537|5(89|583 viz. 89*l.* 11*s.* 8*d.*

57
35
50
20

EXAMPLE VII.

If 100*l.* Lottery Prize be sold for 94½*l.* (viz. 94*l.* 10*s.*) what will a Blank of 6*l.* be sold for ?

That is, as 100 is to 94|5, so is 6 to the Answ.

6
5|670 *viz. 5*l.* 13*s.* 4*d.* $\frac{3}{4}$

† Which is multiplying 5|375 by 100. See Ex. 2. p. 20.

* Which is divided 567|0 by 100. Or 94 might have been first separated for Parts. See p. 61, 62.

EXAMPLE VIII.

WHEN Stock is at 112*l.* 10*s.* how much may be bought for 828*l.*
Viz. as 112*|5* is to 100, so is 828 to the
 Answer

$$\begin{array}{r} 112|5 \\ \times 828000(736) \\ \hline 4050 \\ 6750 \\ (0) \end{array}$$

EXAMPLE IX.

IF 100*l.* Stock is worth 112*l.* 5 what will 736*l.* Stock be worth?

$$\begin{array}{r} 112|5 \\ \times 736 \\ \hline 6750 \\ 3375 \\ 7875 \\ \hline 828|000 \text{ Answer.} \end{array}$$

Of

Of BROKERAGE.

E X A M P L E I.

WHAT is the Brokerage of 2116*l.* 16*s.*
at 1*l.* per Cent.

Answer — 21|168 viz. 21*l.* 3*s.* 4*d.* $\frac{1}{8}$
 At $\frac{1}{2}$ per Cent. 10|584 viz. 10*l.* 11*s.* 8*d.* $\frac{1}{4}$
 At $\frac{1}{4}$ ditto — 5|292 viz. 5*l.* 5*s.* 10*d.*
 At $\frac{1}{8}$ ditto — 2|646 viz. 2*l.* 12*s.* 11*d.*

Here the Sum of the three last is $\frac{7}{8}$ viz. $\frac{4}{8} \frac{2}{8}$ and $\frac{1}{8}$.

For $\frac{3}{8}$ take the $\frac{1}{4}$ and $\frac{1}{8}$, for $\frac{5}{8}$ the $\frac{1}{2}$ and $\frac{1}{4}$,
for $\frac{6}{8}$ the $\frac{1}{2}$ and $\frac{1}{8}$.

If it be required for $2\frac{1}{2}$, $3\frac{1}{2}$ per Cent. &c.
it is only multiplying what it is at 1 per Cent.
by 2, 3, &c. respectively, and adding there-
to the $\frac{1}{2}$, &c. of the 1*l.* per Cent.

Or it may be done by multiplying what it
is 1*l.* per Cent. by the Expression found for
the Parts of the *l.* Sterling ; suppose $\frac{1}{8}$ viz.
12*s.* 6*d.* which Expression per foregoing
is 1625 Parts.

I 2

At

38 *INTEREST* Improved.

$$\begin{array}{r}
 \text{At } 1\text{l. per Cent. as before is } 21|168 \\
 \text{Rate inverted for 2 Places} \quad * \quad 526|0 \\
 \hline
 1270 \\
 42 \\
 11 \\
 \hline
 13|23
 \end{array}$$

$$\begin{array}{r}
 \frac{1}{2} \text{ or } \frac{4}{8} \text{ as before is } 10|584 \\
 \frac{1}{8} \text{ ditto } - \quad 2|646 \\
 \text{Same as above} \quad 13|230
 \end{array}$$

If it had been required for 2, 3, and $\frac{5}{8}$ per C. & c. it would have been prefixing the Integral to the Parts and Multiplying. As in p. 66, 67, 68.

By this Method may the Parts be found in p. 30, 31, &c. as in *Example 6.* p. 31, where the $\frac{1}{16}$ 026 was required to be taken.

$$\begin{array}{r}
 \text{The Expression for } \frac{1}{16} \text{ viz. } 15. 5d. \text{ is } 10625 \\
 \qquad \qquad \qquad |026 + \\
 \hline
 \qquad \qquad \qquad |0016250
 \end{array}$$

Here as the Number of the Parts in both Factors are seven, therefore two Cyphers are prefixed to the Product, to make it consist of so many Places ; see *Rule* p. 63, &c.

* See p. 70.

† The two Places (in dividing by 100) as in p. 61, &c. is performed with all the Numbers in the Table.

Of ANNUITIES IN PERPETUITY.

E X A M P L E I.

IF $740l.$ Principal be given for an Annuity so as to have $6l.$ per Cent. per Ann. for the said Principal. Quere the Annuity?

As 100 is to 6 so is 740 Princip. to the Ans.

$$\begin{array}{r} 6 \\ \hline 740 \\ 44\mid 40 \\ -40 \\ \hline 0 \end{array}$$

viz. $44l. 8s. 0s.$

E X A M P L E II.

IF an Annuity of $44l. 8s.$ be to be sold, so as to be allowed $6l.$ per Cent. per Ann. for the Principal or Purchase-Money. Query the Principal?

As 6 the Rate of Interest is to 100 , so is $44\mid 40$ the Annuity, to the Answer.

$$6\mid 44440(740) \text{ Principal required.}$$

E X A M P L E III.

IF an Annuity of $44l. 8s.$ be bought for $740l.$ what is that per Cent. per Ann. for the Principal?

I 3

As

90 INTEREST Improved.

As 740 the Principal is to 100, so 44|4
the Annuity to the Answer.

740)4440(6 Answer.
(o)

EXAMPLE IV.

IF the Rate of Interest be 6*l. per Cent.*
how many Years Purchase must be given
for any Annuity?

As the Rate is to Unity, so is 100 to the
Answer.

6)100(16|6 Answer, viz. 16 Y. 8 M.
40
40
(4)

Or if you would find the Number of Days
answering to the Parts of a Year, which is
here 6.

Then half of 6, &c. .

will be — — |033333*
Then in the Table agst. 03 is 219 Days.

Remainder 003333
Against next less in Tab. 003288 is 24 Days.

243 ditto.

Remainder 000045

If

* See pag. 55, 56, which is the reverse of pag. 53, 54.

If Curiosity wants the Value of the last Remainder, *viz.* 45, that must be sought for among the Interest of Shillings, and against 41 the next less is 6, to which add a fifth of itself, which will be so many Hours, and the Remainder so many times 12 Minutes, *viz.* 7 Hours 12 Minutes; the last Remainder 4, sought amongst the Interest of the Pence, *viz.* against 3 and 1, or twice 2, will be found 7, which may be taken 8, on Account of the repeating 3, when it will be so many times 6 Minutes, or 48 Minutes, making together 8 Hours; giving for Answer 243 Days 8 Hours.*

When the Principal, or Purchase-Money, and the Annuity are given, the Number of Years Purchase may be found by dividing the former by the latter.

As in Ex. 3d 444)7400(16|6 as before.

2960
2960
(0)

E X A M P L E V.

IF 16|6 Years Purchase be given for an Annuity, what is that *per Cent. per Ann.*

As 16|6 Years Purchase is to Unity, so is 100 to the Answer.

viz.

* All the Cyphers before the several Remainders might have been supposed.

viz. 166) 1000(6 Answer.

1000

(6)

THE following Question is taken from that useful Book of Recreations compiled by *Martin Clare, Esq;* Master of the Academy in *Soho-Square*, where the Answers are only inserted without their Process, for the Exercise of his Pupils; which containing all the Cases of Simple Interest, I have here introduced it, and given the Rules in the Operations through all the Varieties.

A Bond was made *August 7, 1713*, at $6\frac{1}{4}$ per Cent. per Annum, for $1114l. 10s.$ — On *May 11, 1718*, $140l.$ was paid off, and a fresh Bond given for the Remainder at $5l. \frac{1}{4}$ per Cent. per Annum. At the Time the Interest of this last was $21l. 16s. 8d.$ there was paid off $87l. 11s. 9d.$ The old Bond being then taken up, and a new one given for the Residue, which being paid off *September 11, 1724*, the Principal and Interest came to $1409l. 16s. 8d.$ What Rate of Interest did this Bond carry?

This Question has several Conditions: The first is, that from the 7th of *August 1713*, to ditto *1717*, are just 4 Years; next, in the lower Row under *August* in the Table, are

INTEREST Improved. 93

153 Days to the 1st of January in the following Year, and under *May* in the upper Row are 120, making 273 Days, *viz.* from *August 7*, to *May 7*, following: But seeing it is to 11th of *May*, 4 Days must be added, making 277 Days; therefore the first Condition requires the Interest to be found of 1114*l.* 10*s.* for 4 Years and 277 Days, at 6*l per Cent. per Annum.*

Thus the given Principal is 1114*l* 5
The Rate 6 into 4 the No. Years, 24

Interest for 4 Years 267*l* 48*s.*
Interest of 1114*l.* 10*s.* from the Table at 5*l.*

per Cent. for a Day is

15267*l*

Double Rate — 12

At 6 *per Cent.* 183205*(2)*

Days 277

1282435

4946535

50*l* 74778*5*

Int. for 4 Years and 277 Days 318*l* 22778*5*

Principal — 1114*l* 5

Princ. and Int. or the Amount 1432*l* 727*85*

At which time there was paid off 140

Principal due *May 11, 1718* — 1292*l* 72778*5*

Or the Interest for 4 Years, 277 Days, may be found otherwise, *viz.*

Find

94 *INTEREST* Improved.

Find the Expression for 277 Days by p. 51,
and 53.

277 D.

Thus ag. (the next less in Tab.) 219 is 03
Dit. (in 1st Part dit.) — 58 is 7945

Expression — — — 037945

Double is for 277 Days 0|75890

This put for Parts after 4, the Number of Years, is 4|7589, the Expression for 4 Years, 277 Days.

Next the Interest of 1114|5*l.* at 6*l. per Cent.* for one Year (See p. 61, &c.) is 66|87*l.* which multiplied by the Expression for the whole Time, or that by this, as being least in Number of Places, gives the Interest required. Thus,

$$\begin{array}{r}
 4|7589 \\
 66|87 \\
 \hline
 333123 \\
 380712 \\
 \hline
 285534 \\
 285534 \\
 \hline
 318|227643 *
 \end{array}$$

Either of which Ways, in like Cases, may be used at Pleasure, or as shall be found most convenient.

The

* The Difference between this and the former is of no Signification, and is owing to a small Defect in the Expression for the Number of Days.

The next Condition is, that when this Principal had gained $21\ l.\ 16\ s.\ 8\ d.$ at $5\frac{1}{4}$ per Cent. per Ann. $87\ l.\ 11\ s.\ 9\ d.$ was then paid off.

To find the Time that any given Principal, at any given Rate, shall gain a given Interest.

RULE.

Multiply the Principal by the Interest of $1\ l.$ for a Year at the said Rate, next divide the given Interest by the Product, and the Quotient is the Answer.

First the double of the Rate is — — 10|5
 And per Tab. the Int. of $1\ l.$ for a Year
 at 5 per Cent. (See p. 42.) is — — |05
 Int. ditto at $5\frac{1}{4}$ per Ct. (See p. 23, 87, 88) |0525

Principal	—	—	1292 727 785
Int. inverted for 4 Places			5 250,0
(See p. 67, 70)			<hr/>
		6463 64	
		258 54	
		64 64	
Product with 4 Places	<hr/>	67 86 82	

Or

96 *I N T E R E S T* Improved.

Or divide by 100 * 12|92727785

At 5 per Cent. 5

64|63638925

$\frac{1}{4}$ Principal, &c. 3|23181946

At $5\frac{1}{4}$ as before 67|6820871

The Interest, *viz.* 21|83 is *per* the Rule to be divided by the said Product, *viz.*

678|6|8|2)218333|3(|3217 Parts of a Year,

147287 *viz.* 117 Days,

11551 &c. See p. 90.

4764

(13)

The 117 Days added to *May 11*, the Date of the Bond, points out *Sept. 5* following, (See p. 3) when the aforesaid 87*l.* 11*s.* 9*d.* was paid off.

Thus the given Principal was 1292|727785

Int. of ditto to *Sept. 5*, &c. 21|833333

Princ. and Int. or the Amount, 1314|5611(18

Paid off then — — — 87|5875

Remains due — — — 1226|9736

The other Condition is, that on the 11th of *September 1724*, *viz.* for 6 Years and 6 Days, this Sum, with its Interest for that Time amounted to 1409*l.* 16*s.* 8*d.*

It

* See Note p. 61.

It is required to find what was the Rate of Interest.

R U L E.

FROM the given Amount subtract the given Principal, the Remainder will be the Interest for the said Time; next divide the Remainder (*viz.* Interest) by the Product of the Principal multiplied into (or by) the Time, the Quotient will be the Rate of Interest for *1 l. per Ann.* which multiplied by 100 gives the Answer *per Cent. per Ann.*

The Amount here given is	1409 8333
Principal ditto,	1226 9736
Remainder, or Interest,	<hr/> 182 8597

The Time given is 6 Years and 6 Days; next to find the Expression for 6 Days (*See p. 53*) in the Table against 12 (the Double) is 1644, but two Cyphers are to be (or supposed) prefix'd, and *per Rule* (*p. 51, 52, 53*) one seperated to the left Hand gives |01644, which with the 6 Years is 6|01644, the Expression for the whole Time.

98 *INTEREST* Improved.

The Principal, as before, is 1226|9736
 Time inv. for 4 Places in the Prod. 446106

$$\begin{array}{r} 73618416 \\ 122697 \\ 73618 \\ 4908 \\ \hline 491 \end{array}$$

 Product of Prin. mult. per the Time 7382|0130

Which *per* the Rule is the Divisor, and
 182|8597 the Dividend. Thus

7|3|8|2)182|8597(|024771, which multiplied
 35219 by 100 gives
 5691 2|4771 (see p. 19)
 524 viz. 2*l.* 9*s.* 6*d.*
 7 Ans. *per C. per A.*
 (0) &c.

If it is required to prove this, the Question will be, if 100*l.* gain 2*l.* 9*s.* 6*d.* in a Year, what will 1226|9736*l.* gain in 6 Years and 6 Days?

Or if 1*l.* gain 1024771 in a Year, what will 1226|9736 gain in the above Time?

The

INTEREST Improved. 99

The Principal as before	1226 9736
Invert. for 4 Places of Pts. in the Prod.	<u>177420 0</u>
	245395
	49079
	8589
	859
	12
<i>Viz.</i> for one Year,	<u>30 3934</u>
Time inverted for 4 Places of Parts in the Product,	<u>44610 6</u>
	1823604
	3039
	1823
	121
	12
Answer	<u>182 8599</u>

If the Operations had been for more Places of Parts in the Product than 4, the fourth Place would have been true; but that is no Way material, it being but a thousandth Part of a Farthing Odds.

If the second Condition be required to prove back, *viz.* for 117 Days, &c. it will be necessary for Exactness to have Regard to the Hours or Parts of a Day. Thus

100 *INTEREST Improved.*

The Parts as there
found were — 3217 *
Ordered, &c. 1016085
In the Tab. against 101 - - is 73 Days
Rem. - - - 6085
Dit. — — — — 6027 44 Days
Rem. — — — 58, 117 Days
— H. /
† Dit. among the Sh. — — 55 8 viz. 9 36
Dit. am. the Pence — — — 3 is 5 dit. — — 30
H. /
Viz. 10 6

To find the Expressions for the Hours and Minutes, divide the Min. by 6, adding one more to the Quote if the Remainder be 3 or upwards ; next, annex this Quote to the Hours as Parts, which divided by 24 this last Quote will be the Answer. ||

Thus 24)10|1(|42 the Answ. required.

50

(o)

Therefore the Expression for the Days and Hours, &c. is 117|42

The State of the Question now is, What is the Int. of 1292 l. 14s. 7d. for 117|42 Days, at $5\frac{1}{4}$ l. per Cent per Annum.

The

* See p. 96.

† See p. 90, 91.

|| Otherwise multiply 101 by 4, adding to the Product one sixth of the said 101, separating all for Parts, the like with others.

INTEREST Improved. 101

The Int. from the Tab. at *5 per Ct.*

for a Day is —————— 177086

(and the double Rate 10 $\frac{1}{2}$) ——————

Dit. mult. by 10 (wh. gives 7 Places) is 1770860

$\frac{1}{2}$ Int. at *5 per Cent.* — 88543

Int. at $5 \frac{1}{4}$ per Cent. for a Day — 18594(03*)

No. Days inv. for 3 Pl. in the Prod. 24711

18594

1859

1302

74

4

Viz. 21*l.* 16*s.* 8*d.* — + 21|833 An.

Or the Interest at *5 l. per Cent.* may be reduced to any other Rate universally as in *Page 65.*

Thus the Expression for double the Rate (*see P. 42*) is 10|5 by which multiply the Int. for a Day at *5 p.Ct.* viz. 177086

$\frac{885430}{18594030}$ (See P. 36)
Prod. by 105

Here the Product consists of || 8 Places of Parts, but the first 5 are sufficient for Use.

Another Condition may be added to these, as, What Principal at *6 per Cent. per Annum*

K 3 shall

* See Note p. 10, & p. 23.

† See p. 96.

|| viz. 7 by p. 23. and one for that in the Rate. See p. 88.

shall in 4 Years and 277 Days amount to
 $1432\text{l. } 14\text{s. } 6\text{d. } \frac{3}{4}$.

R U L E.

MUltiply the Time by the Rate or Interest given of 1*l.* for a Year, to the Parts of which Product || prefix (or † add) an Unit, by which dividing the given Amount, gives the Answer required.

The Expression for 277 Day (*see p. 53, 90*) is
 $1|7589$, and the 4 Years prefix'd is $4|7589$
 The given Rate of 1*l.* for a Year $|06$

(*see p. 23, &c.*)

Product with Unity prefixed $1|285534$

The Expression for the given Amount is
 $1432|728125$, both which ordered will be

$128|5|5|3|4)1432728125(1114|5$ Answer.

$\begin{array}{r} 147194 \\ 16641 \\ 5786 \\ 644 \\ (1) \end{array}$

|| When the Product consists of all Parts.

† When it consists of Integers and Parts.

* See p. 78.

S U P P L E M E N T.

The Construction of the Table.

IT has been observed (*p. 42.*) that 105 is the Expression for the Interest of $1\text{l}.$ for 365 Days, at $5\text{l. per Cent. per Ann.}$

Therefore dividing 105 (*annexing Cyphers to the right Hand) by 365 , the Quotient will be the Expression of the Interest of 1l. for a Day at that Rate.

But 365 and 105 are both divisible by 5 , and leave no Remainder; their Quotes, therefore, *viz.* 73 and 101 , divided in the same Manner, will give an equal Quotient.

This is the Converse to Lemma *p. 71.*, as is plain by multiplying 73 and 101 back by 5 :

Thus $73|0100(\dagger 0001369863$

270
 510
 720
 630
 460
 220
 (1)

Here

* See *p. 30, 31.*

† See *p. 80.*

Here the last Remainder is the same as at first in the Dividend ; and by dividing on it may be observed, that the Quote will continually repeat in the same Order as dotted ; which here needs no farther Consideration.

Next as 136 is followed by 9, and that again by 8, &c. * it may mostly, without any significant Error, be taken 1000137, answerable to 137 in the Table against 1*l.* with three Cyphers supposed.

Again, from 137 . . .
 Take the said Quote, 1369863
 Remainder, 0000137

Hence it is plain, that if 137 be placed the fifth Place to the right Hand under itself, (supposing Cyphers) and subtracted therefrom, it will give the aforesaid Quote, viz. the Interest of 1*l.* for one Day, at 5 per Cent. per Ann.

Thus 137 . . .
 Same as before, 1369863 137

From whence it is easy to conceive, that any Product made by 137, set a fifth Place under itself, and subtracted in like Manner, will

* See p. 15.

INTEREST Improved. 105

will give the same as if it had been multiplied by 1369863, the Interest of 1*l.* for one Day.

It is obvious, that if the Interest of 1*l.* for one Day, be multiplied by any Number of Pounds, the Product will be the Interest of the said Number of Pounds for one Day, which leads to the following Problems.

P R O B. I.

WHAT is the Interest of 67*l.* for a Day, at 5*l.* per Cent. per Ann.

As the greater Factor is 137
Multiply by 67

9179

As there are always three Cyphers supposed prefixed to 137, there will, when the given Principal is Integral, be six Places of Parts in the Product, (see p. 5.) so that two Cyphers are here to be supposed prefixed.

Next, in general, there need only the last left Hand Digit in the Product be set a fifth Place below itself, and subtracted.

Thus, 9179
 9

9178|1

Which

Which Product will then consist of seven Places; but as six are sufficient, and the last Place under 5, it may be omitted, and is the same as in the Table against 67, viz. 9178.

P R O B. II.

WHAT is the Interest of 8*l.* for a Day at 5 per Cent. per Ann.

$$\begin{array}{r} 137 \\ 8 \\ \hline 1096 \end{array}$$

Here it may be seen, that if 1 be taken as before the sixth Place would be 5, and the seventh 9, in which * Case the sixth might have remained as at first; from whence it follows, that when the last left Hand Digit in the Product is 5 or upward, the last to the right Hand is to be made one less, and when under 5 to remain as it is, &c. And the above 1096 the same as against 8 in the Table.

P R O B. III.

IT may likewise be observed, that the several Interests of 1*l.* in the first Part of the Table, as far as 37*l.* are Multiples of

137;

* See p. 23.

137; but against 37 is 5068, and 137 into 37 gives 5069.

But from the preceding Remark, as the last left Hand Digit is 5, &c. the last right Hand must be made an Unit less, when it becomes, as in the Table, the like with the succeeding Interests, to end Part Ist.

P R O B. IV.

THE Interest for the Shillings may likewise be found in the same Manner.

$$\begin{array}{r} \text{Multiply} \quad - \quad - \quad 137 \\ \text{By the Expression for a Shilling} \quad * \quad \underline{105} \\ \hline 685 \end{array}$$

Here, as there are six Places of Parts in the Multiplicand, 137 with three Cyphers supposed, also two in the Expression for a Shilling, there must be eight in the \dagger Product, and consequently five Cyphers supposed prefixed thereto; next, as 8 in the seventh Place exceeds 5, the 6 may be taken 7, as in the Table, with five Cyphers supposed (*see p. 4.*)

* See p. 42.

† See p. 88.

P R O B . V.

$$\begin{array}{r}
 \text{Again multiply} \quad \underline{\hspace{2cm}} \quad | \quad 137 \\
 \text{By the Expression for } 19 \text{ Shillings} \quad | \quad 95 \\
 \hphantom{\text{Again multiply} \quad \underline{\hspace{2cm}} \quad |} 685 \\
 \hphantom{\text{Again multiply} \quad \underline{\hspace{2cm}} \quad | \quad 137} \underline{\hspace{2cm}} \quad 1233 \\
 \hphantom{\text{Again multiply} \quad \underline{\hspace{2cm}} \quad | \quad 137} \quad | \quad 130(15)
 \end{array}$$

Here are only three Cyphers to be supposed, and as the seventh Place is under 5, therefore 130 is the Expression for 19 Shillings, with three Cyphers supposed, as in the Table, (*see p. 4.*)

P R O B . VI.

THE Expression for a Shilling, *viz.* 685, divided by 6, gives 114, &c. with five Cyphers supposed; therefore 1, as in the Table, is the Expression for Two-pence, and from this may those for all the Pence, &c. be found, as in p. 11.

Or this may be done by reducing the Pence, &c. to Farthings, as in p. 42, and multiplying the Expression by 137.

P R O B .

PROB.

P R O B. VII.

WHAT is the Expression for the Interest of 7 d. for a Day, at 5 per C. per Ann.

The Expression for 7 d. is 102917

$$\begin{array}{r} 137 \\ \hline 20419 \\ 37921 \\ \hline 3199629 \end{array}$$

Here are eleven Places to be considered for the Product, and five Cyphers supposed prefixed, but for Use, six Places at most being sufficient, the 3 is separated for that Purpose; next, seeing that two nines follow, it may by the foregoing safely be taken 4, answering to twice 3 d. $\frac{1}{2}$ in the Table. The like with others.

P R O B. VIII.

WHAT is the Expression for the Interest of 19 s. 9 d. for a Day, at 5 l. per Cent. per Ann.

L

The

The Expression for 19*s.* 6*d.* is |9875
 Multiply by ————— |137
 69125
 128375
 —————
 135|2875

In the Table against 19*s.* is 130, and against 9*d.* viz. 5*d.* and 4*d.* are 3 and 2, making 135, with three Cyphers supposed, supposed, as above.

These Multiplications may likewise be greatly contracted (*see p. 66, 67*) by placing the 7 under that Place for the Number of Parts designed for the Product, and inverting 13 to the right Hand, as follows.

P R O B. IX.

WHAT is the Interest of 63*l.* 13*s.* 5*d.* for a Day, at 5*l.* per Cent. per Ann.

Principal ordered is 63|67083

Here it may be observed, that if all was to be multiplied by 137, there would be eleven Places of Parts in the Product; but as six are the most requisite, and always enough, place the 7 under the Unit's Place of the Integral

I N T E R E S T Improved. 111
tegral Part of the Principal, inverting 13 to
the right Hand.

Thus 63|67083
 731

Where you may omit multiplying by 1, and begin with the 3, observing the Carriage of 7, the right Hand Digit in the Principal; next, to this Product add the said right Hand Digit, proceeding on as in multiplying by 13 in one Line (*see p. 34*) ; lastly, multiplying by 7 according to the Rule, &c. you will have the Product of six Places of Parts required.

Principal, &c.	63	67083
13 inverted		731 +
		<hr/>
	8277	
	446	
	<hr/>	
	8723	

Next, by the foregoing 8 placed a fifth Place, &c. and subtracted, leaves 8722 with two Cyphers supposed prefixed, &c. which will be found to agree with the Table.

L 2

When

+ When the last right Hand Figure in the inverted Multiplier is 2, &c. you may take the double, &c. of the right Hand Figure in the Multiplicand (*see p. 35*) by which Rule, multiplying by the Number of Days, as in *p. 70*, &c. a Line may be contracted.

112 *INTEREST* Improved.

When the Principal consists all of Parts, you must put or suppose a * Cypher before them, which will then be the Unit's Place, operating in other respects as before.

P R O B. X.

WHAT is the Interest of 19*s.* for a Day at 5 per Cent. per Ann.

$$\begin{array}{r}
 \dfrac{\dfrac{\dfrac{\dagger \text{ Principal, \&c.}}{0|9875}}{731}}{128} \\
 \hline
 7 \\
 \hline
 135
 \end{array}$$

With three Cyphers supposed, &c. the same as before ; the like with all others.

In the second Part of the Table against 73 is 101, the Reason of which may be easily seen from p. 42, and the first of this Supplement.

And by taking Multiples of these ; are all the Numbers formed in the said second Part.

But they may be also formed, following the Rule, in multiplying by 137.

* Which is the Reverse to p. 70.

† See Prob. 8.

P R O B.

P R O B. XI.

WHAT is the Interest of 73*l.* for a Day, at 5*l.* per Cent. per Ann.

$$\begin{array}{r}
 137 \\
 73 \\
 \hline
 411 \\
 959 \\
 \hline
 10001
 \end{array}$$

Here I placed a fisth Place to the right Hand, and subtracted, leaves 10000, and the Cypher prefixed to make up six Places for the Product, it becomes 101, as in the Table.

P R O B. XII.

WHAT is the Interest of 2263*l.* for a Day, at 5*l.* per Cent. per Ann.

$$\begin{array}{r}
 2263 \\
 127 \\
 \hline
 15841 \\
 29419 \\
 \hline
 310031 \\
 31 \\
 \hline
 1310000
 \end{array}$$

the same as in the Table.

L 3

If

If the Principal had consisted likewise of Shillings, Pence, &c. you must have operated as in Prob. 9. and so with all others.

If any other Rate, or Number of Days, should be required, you must proceed in all Respects as before taught.

P R O B. XIII.

WHAT is the Interest of 100000*l.* for 22 Days at 5 *per Cent. per Ann.*

First, 137 by the Principal gives 13700000
Product placed a fifth, &c. 137
Int. for a Day at 5*l. per Cent.* 13|69863*

Then by Rule (*p. 23.*) this is to be multiplied by double the Rate, and a Place more separated for Parts, &c. which let first be separated thus,

1|369863

Next, multiply this by double the Rate into the Time, (*viz.* 132) so as to have only four Places of Parts in the Product.

* See Ex. 5. p. 22.

Thus

Thus	1 369863
Double Rate, &c. inverted,	<u>231</u>
	1780822
	<u>27397</u>
	180 8219*

Any Annuity given, to find what that is
per Day.

Dividing the Annuity by 365, or first by 5, and that Quote by 73, gives the Answer required.

Otherwise,

First double the Annuity, next separate one Integral Place to the right Hand, which makes one Place more to the Parts (if any before) lastly multiply this by 10137, &c. †, the Product gives the Answer required.

P R O B. XIV.

A N Annuity of 54*l.* 15*s.* what is that
per Day?

Viz.

* See p. 33.

† Which is the Quote of Unity divided by 73, &c.]

Viz. 54|75 ordered by the Rule is

10 95
0137
<hr/>
7665
14235
<hr/>
150015

Product placed, &c.

Viz. 3 Shill. the Answer,

— —
— —
15 ...†

By this Rule may the Expression for any Number of Days of a Year be also found.

P R O B. XV.

WHAT is the Expression for 277 Days?

Double ditto ordered, &c. is

55 4
0137
<hr/>
3878
7202
<hr/>
175898
—
76
<hr/>
1758904*

Product placed, &c.

Answer for six Places

† See Ex. 1. p. 51.

* See p. 94.

P R O B.

P R O B. XVI.

WHAT is the Expression for one Day of
a Year?

$$\begin{array}{r} \text{First, } - & |0\cdot37 \\ \text{Day ordered, \&c.} & |2 \\ \hline & |00274 \end{array}$$

Here a Cypher is prefixed to the Product,
to make it equal to the Number of Parts in
both Factors. (See p. 88)

As |00274 * is the Expression for one Day,
any Number of Days also multiplied thereby
will give the Expression required, observing
to place the Product a fifth under itself, &c.
whence you may have it for all the Places ;
but 5 or 6 is ever sufficient.

Any daily Sum given, to find what that is
per Ann.

Multiplying the Expression by 265, or
by 5, and that Product by 73, gives the
Answer.

Otherwise,

Separate the first Place of Parts to the left
Hand, next multiply the half thereof by 73,
which gives the Answer required.

* Which is the Quotient of Unity divided by 365, &c.

P R O B. XVII.

AT 3 Shillings *per Day*, what is that *per Ann.*

Expression for 3 Shill. &c. 1|5
 Half |75
 73
 —
Viz. 54*l.* 15*s.* Answer. 54|75||

P R O B. XVIII.

AT 3*l.* 13*s.* 6*3/4 d.* *per Day*, what is that *per Ann.*

The Expression, &c. is 36|78115
 Half 18|390625
 73
 —
 1324|515625* Answ.
Viz. 2342*l.* 10*s.* 3*3/4 d.*

By this Method may the Number of Days answering to any Expression be found.

P R O B. XIX.

WHAT are the Number of Days answering to 1758904†

Ex-

|| See p. 56.

♦ Multiply by 4, as in p. 40.

† See p. 116.

$$\begin{array}{r}
 \text{Expression ordered, \&c.} \quad 7|58904 \\
 \text{Half} \quad 3|79452 \\
 \hline
 & \quad 73 \\
 & \hline
 276 | 99996
 \end{array}$$

Answer 277 Days (*see p. 15*)

P R O B. XX.

$$\begin{array}{r}
 \text{WHAT are the Number of Days answer-} \\
 \text{ing to} \quad |3217^* \\
 \text{Half, \&c.} \quad 1|6085 \\
 \hline
 & \quad 73 \\
 \text{Answer 117 Days, \&c.} \quad 117 | 4205 \\
 & \hline
 & \quad 24 \\
 \text{Hours,} \quad 10 | 0920 \\
 & \hline
 & \quad 60 \\
 \text{Minutes, \&c.} \quad 5 | 5200
 \end{array}$$

Here the Parts of a Day are multiplied by 24, which gives the Hours, and the Parts of an Hour by 60, which gives the Minutes; the like with all others; but such Exactness is seldom or never wanted.

P R O B. XXI.

WHAT are the Number of Days answering to 16, in p. 90.

The

* See p. 96.

The half ordered becomes $\frac{3}{2}$, an Integral,
by which multiply $\frac{73}{3}$

$$\text{Thus} \quad \begin{array}{r} 3 \\ \hline 219 \end{array}$$

Which must be divided by 9, and the Quotient
added. (*see p. 46*)

$$\begin{array}{r} 9)219. \\ 24\cancel{1}\cancel{3} \\ \hline 243\cancel{1}\cancel{3} \end{array} \text{ True Product.}$$

Otherwise,

Set the Product a Place farther to the left
Hand, supplying the Vacancy with 0, when
dividing the same by 9, you will have the true
Product at once.

$$\begin{array}{r} \text{Thus} \quad \begin{array}{r} 73 \\ 3 \\ \hline 9)2190 \end{array} \\ \text{L} \quad 243\cancel{1}\cancel{3} \end{array} \text{ True Product, as before.}$$

Next multiply 24 by $\frac{1}{3}$ Parts for the Hours.

$$\begin{array}{r} \text{Thus} \quad \begin{array}{r} 3 \\ \hline 9)72\cancel{0} \\ 8\cancel{0} \end{array} \\ \text{viz. } 8 \text{ Hours.} \end{array}$$

If

INTEREST Improved. 121

If the Months in a Year, 12, be multiplied by $\frac{1}{6}$, the first Expression, the true Product will be the Number of Months answering thereto.

Thus 12

$$\begin{array}{r} | \\ \frac{1}{6} \\ \hline \end{array}$$

$$\begin{array}{r} 9)72\mid 0 \\ \hline \end{array}$$

Months required 8|0

P R O B. XXII.

WHAT is the Interest of 225*l.* 16*s.* $7\frac{1}{2}$ *d.* for 327 Days at 5 per Cent.

Expression, &c. 225|83125

$$\begin{array}{r} 731 \\ \hline 29358 \\ 1581 \\ \hline 1030939 \end{array}$$

Product a Fifth, &c. 3

$$\begin{array}{r} 1030936 \\ 327 \\ \hline 92808.. \\ 835272 \\ \hline 10116072 \end{array}$$

Viz. 10*l.* 2*s.* 4*d.* nearly.

A

M

This

122 *INTEREST* Improved.

This Contraction in multiplying by 327, is just the Reverse to that in pages 37 and 38; for 3 in 27 being 9 times, it is first multiplied by 3, (*viz.* 300) and that again by 9, which is very plain and obvious.

It sometimes happens that any Digit may be exactly contained in the three next preceding or succeeding, when you may operate in all respects as before, *viz.* suppose any Number to be multiplied by 1449, here 144 divided by 9 gives 16, therefore first multiplying by 9, and that Product by 16 in one Line, will give the Product required.

Or if the Multiplier be 9144, it would be first multiplying by 9, and that Product again by 16, as in the last Problem.

All which, at any time, may be easily conceived by those who understand but the first four Rules of Arithmetic.



A P.



APPENDIX.

IN Page 67, &c. there is given a Method for Contracting in Multiplication, by inverting the Multiplier: But as the same may be performed without, I shall here give the Methods, that either may be used, as shall be best approved of.

In the common way of Multiplication, it is always usual to begin with the Unit's Place, &c. But it may as well be begun with the highest to the left Hand, Regard being had to the Value of the Place it possesses.

EXAMPLE I.

CASE I.

234

234

936

702

468

54756

CASE II.

234

234

468 ..

702 .

936

54756

CASE III.

234 ..

432

468 ..

702 .

936

54756

M 2

L

124 *INTEREST Improved.*

In the third Case, where the Multiplier is inverted, it falls two Places to the Right Hand beyond the Multiplicand, to which, by the Rule of Inverting, must be annexed (or supposed, as above by Dots) so many Cyphers to the Right Hand of the Multiplicand, till it becomes equal in Places with those of the inverted Multiplier.

Hence it is evident, by annexing two Cyphers to the Right Hand of the Multiplicand, is multiplying by 100; next, multiplying by 2, beginning at the Place over it, the Product will be equal to that in the second Case multiplied by 200; again, multiplying by 4, beginning at the Place over it, when one Cypher is only to be considered as annexed to the Multiplicand, which is multiplying the same by 10, and that again by 4, is multiplying by 40, as in the second Case, &c. all which is very obvious.

E X A M P L E II.

LE T 45|4789 be multiplied by 6|235, so as to have only three Places of Parts in the Product. †

CASE

† Which may be also for any other Number of Parts, or none. See p. 67, 70.

CASE I.	CASE II.
45 4789	45 4789
6 235	Multip. 532 6 inverted
—	—
272873	272873
9096	9096
1364	1364
227	227
—	—
283 560	283 560

Here it is to be observed (Case I.) as three Places of Parts only are required in the Product, that, instead of setting 6, the Unit's Place of the Multiplier, under 8, the third Place of Parts in the Multiplicand, and inverting; the Multiplication is begun with 6 into 8, with the Addition of 5, the Carriage of 9 to the Right Hand, and so proceeding on gives 272873.

The next Figure to multiply by is here but two tenths, so much therefore of the Multiplicand, *viz.* 45|4789 is only to be taken.

* One tenth whereof is 4|54789, which now is to be multiplied by 2, so that three Places of Parts only may be in the Product;

M 3 from

* See Note † p. 20.

126 INTEREST Improved.

from whence it is plain you must begin at 7, having regard to the Carriage as before, (and under which in the second Case you find the 2 to stand) and proceeding on as before you will have that Product accordingly.

The following Figure is but three hundredth Parts, and so much of the Multiplicand is to be taken.

† One hundredth Part thereof is 1454789, which is to be multiplied by 3, and that only three Places of Parts may be in the Product, it is obvious you must begin multiplying at 4 in the Multiplicand; under which you find it in Case II.

Lastly, 5 is but five thousand Parts, and one thousandth Part of the Multiplicand is 10454789, and by the foregoing it is evident you must begin the Multiplication at 5 therein, under which also it stands in Case II.

From hence it may be easily observed, that after your first Multiplication you drop a Place to the Right Hand in the Multiplicand, when you begin with the second in the Multiplier, and so on each Time, till all is finished.

It may likewise be observed, that the Multiplication may be first begun with the last

† See Note * p. 61.

last Place to the Right Hand in the Multiplier, the Multiplicand being first formed, (or conceived so) accordingly, thus 10454789, one thousandth Part of the Multiplicand (as above) is now to be multiplied by 5, that three Places of Parts may be in the Product; whence it is obvious you must begin multiplying at 5 in the Multiplicand Regard being had in all Cases to the Carriage of a Place or two to the Right Hand, as before taught); and when you multiply by 3, you must begin at 4 in the Multiplicand; by 2 with the 7; and by 6 with the 8; just in all respects the Reverse of the last.

Or in the inverted Order you may begin multiplying with the 5 first, and so on, which directly answers the same Purpose. Thus,

$$\begin{array}{r}
 45|4789 \\
 532|6 \\
 \hline
 227 \\
 1364 \\
 9096 \\
 272873 \\
 \hline
 283|560
 \end{array}$$

E X A M P L E III.

SUPPOSE 7645|4789 to be multiplied by 6546|235, to have only three Places of Parts in the Product.

CASE I.

$$\begin{array}{r} 7645|4789 \\ 6546|235 \end{array}$$

CASE II. inverted.

$$\begin{array}{r} 7645|4789.. \\ 532|6456 \end{array}$$

In the first Case, if you begin multiplying with 6, the highest Place in the Multiplier, which is 6000, the Multiplicand being first multiplied (or conceived) by 1000, will be 7645478|9, which is now to be multiplied by 6, so that the Product may have but three Places of Parts ; two Cyphers therefore must be annexed (or supposed) after the 9 for that Purpose, and then multiplied by 6, which is answered by the Dots in Case II. inverted. These Examples being thoroughly considered, the Reason for inverting the Multiplier evidently appears ; which to Tyro's and Persons not very expert, will be found much the surest Way, and the least liable to Mistakes.

F I N I S.

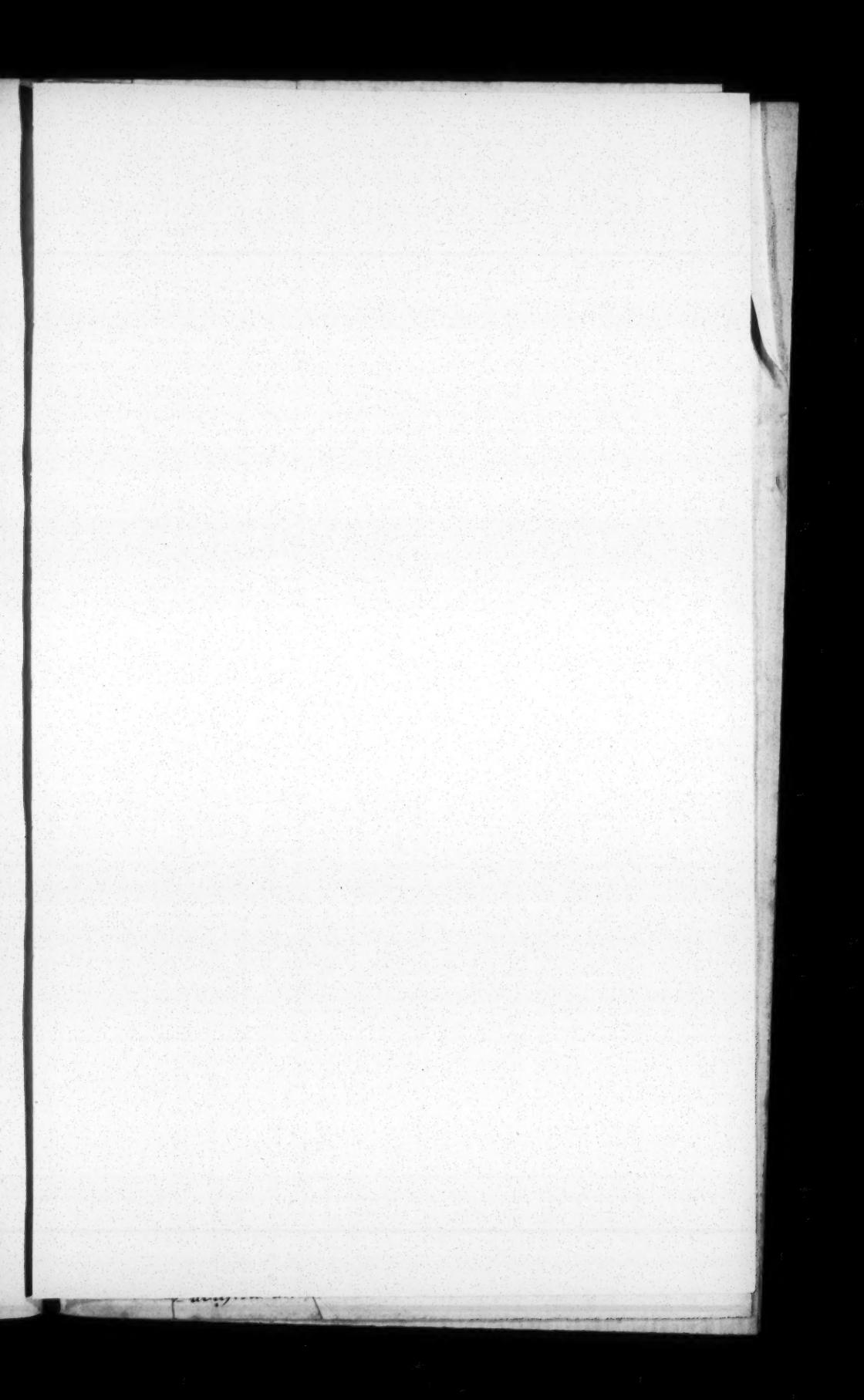


Table to find the

Janua	Februa	March	April	M
0	3	59	90	32
365	334	306	275	24

Table for finding the

at 3 P^r Centum P^r. An

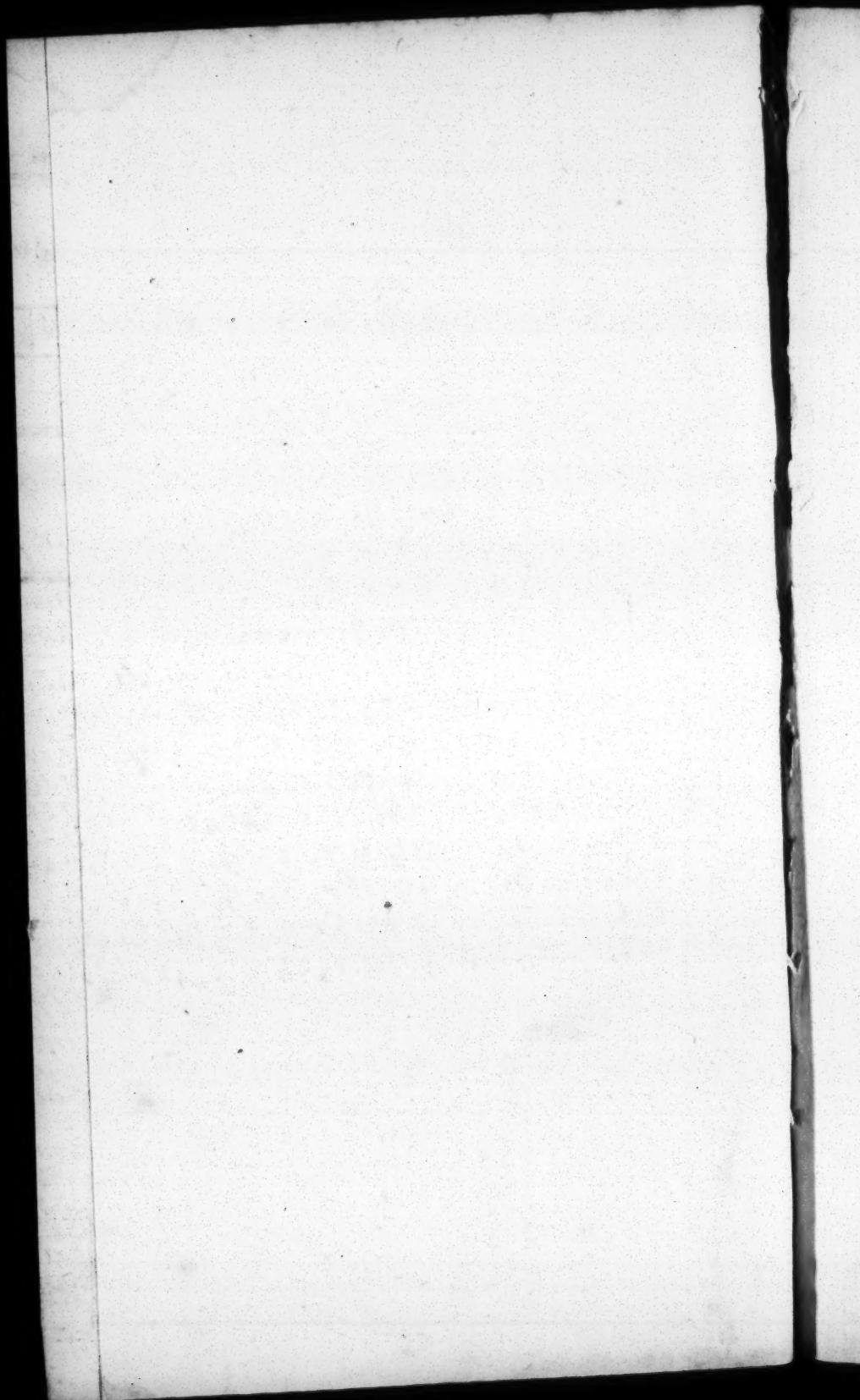
Prin Parts.	Interest £.s Parts	Prin £.s Parts	Interest £.s Parts	Prin £.s Parts
2	1	1	137	26 3562
32	2	2	274	27 3699
4	2	3	411	28 3836
5	3	4	548	29 3973
10	6	5	685	30 4110
11	6	6	822	31 4247
1	7	7	959	32 4384
2	14	8	1096	33 4521
3	21	9	1233	34 4658
4	27	10	1370	35 4795
5	34	11	1507	36 4932
6	41	12	1644	37 5068
7	48	13	1781	38 5205
8	55	14	1918	39 5342
9	62	15	2055	40 5479
10	68	16	2192	41 5616
11	75	17	2329	42 5753
12	82	18	2466	43 5890
13	89	19	2603	44 6027
14	96	20	2740	45 6164
15	103	21	2877	46 6301
16	110	22	3014	47 6438
17	116	23	3151	48 6575
18	123	24	3288	49 6712
19	130	25	3425	50 6849

and the Number of Days from one Month
to another &c. as

April	May	June	July	Aug ^t	Sept ^r	Octo. ^r	Nov. ^r	Decem.
90	120	151	181	212	243	273	304	334
275	245	214	184	153	122	92	61	31

ing the Interest of any Sum for one Day
P. Annum and thence for any Time & Rate.

in Parts	Interest P. Parts	Prin. Pounds	Interest P. Parts	Princip. Pounds	Int. P. Parts	Interest P. Parts	Princip. Pounds	Int. P. Parts	Princip. Pounds	Int. P. Parts
6	3562	51 69 86		73 .01	1898 .26	3723 .51	5548 .76			
7	3699	52 71 23		146 .02	1971 .27	3796 .52	5621 .77			
8	3836	53 72 60		219 .03	2044 .28	3869 .53	5694 .78			
9	3973	54 73 97		292 .04	2117 .29	3942 .54	5767 .79			
0	4110	55 75 34		365 .05	2190 .30	4015 .55	5840 .80			
1	4247	56 76 71		438 .06	2263 .31	4088 .56	5913 .81			
2	4384	57 78 08		511 .07	2336 .32	4161 .57	5986 .82			
3	4521	58 79 45		584 .08	2409 .33	4234 .58	6059 .83			
4	4658	59 80 82		657 .09	2482 .34	4307 .59	6132 .84			
5	4795	60 82 19		730 .10	2555 .35	4380 .60	6205 .85			
6	4932	61 83 56		803 .11	2628 .36	4453 .61	6278 .86			
7	5068	62 84 93		876 .12	2701 .37	4526 .62	6351 .87			
8	5205	63 86 30		949 .13	2774 .38	4599 .63	6424 .88			
9	5342	64 87 67		1022 .14	2847 .39	4672 .64	6497 .89			
0	5479	65 89 04		1095 .15	2920 .40	4745 .65	6570 .90			
1	5616	66 90 41		1168 .16	2993 .41	4818 .66	6643 .91			
2	5753	67 91 78		1241 .17	3066 .42	4891 .67	6716 .92			
3	5890	68 93 15		1314 .18	3139 .43	4964 .68	6789 .93			
4	6027	69 94 52		1387 .19	3212 .44	5037 .69	6862 .94			
5	6164	70 95 89		1460 .20	3285 .45	5110 .70	6935 .95			
6	6301	71 97 26		1533 .21	3358 .46	5183 .71	7008 .96			
7	6438	72 98 63		1606 .22	3431 .47	5256 .72	7081 .97			
8	6575	End of		1679 .23	3504 .48	5329 .73	7154 .98			
9	6712			1752 .24	3577 .49	5402 .74	7227 .99			
0	6849	Part i st		1825 .25	3650 .50	5475 .75	7300 .100			



ERRATA.

P. 12, Ex. I. for 101 r. 101.
17, line 8, 2d r. 1st.
18, 4, dele of.
33, 6, for 108 r. 180.
46, 18, * r. †.
ib. 20, † r. *.
55, 10 d. r. 10 s.
66 9, should be a Place to the left.
74, 11, for 253 r. 250.
88, 17, 1 s. 5 d. r. 1 s. 3 d.
89, 15, 44440 r. 4440.
102, 18, 16641 r. 18641.
110, 1, 19 6 r. 19 9.
112, 6, 19 s. r. 19 9.
114, 9, 5 per Cent. r. 3 per Cent.
118, 14, & 15, for 1324 r. 1342, &c.

